

**Testing the FoF**  
**(not the meeting, but the algorithm)**

**Ariel Zandivarez**

# Collaborators

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**Brasil: Claudia Mendes de Oliveira, Renato Dupke**

**España: Narciso Benitez, Begoña Ascaso**

**and JPAS-team.**

# Aim of the work

- **Construct mock catalogues for the future JPAS.**
- **Test algorithms to identify galaxy groups.**
- **Predict purity and completeness of the resulting groups samples.**
- **Test different statistical tools.**

# How to construct a mock catalogue?

**N-body numerical simulation**

```
graph TD; A["N-body numerical simulation"] --> B["assigning galaxies  
DM=Gal or  
bias model"]; A --> C["building galaxies  
semianalytically"]; A --> D["simulating the  
gas component"];
```

**assigning galaxies  
DM=Gal or  
bias model**

**building galaxies  
semianalytically**

**simulating the  
gas component**

# How to construct a mock catalogue?

**N-body numerical simulation**



```
graph TD; A["N-body numerical simulation"] --> B["building galaxies semianalytically"]
```

**building galaxies  
semianalytically**

# N-body cosmological numerical simulation: The Millennium Run

## Virgo Consortium (Springel et al 2005)

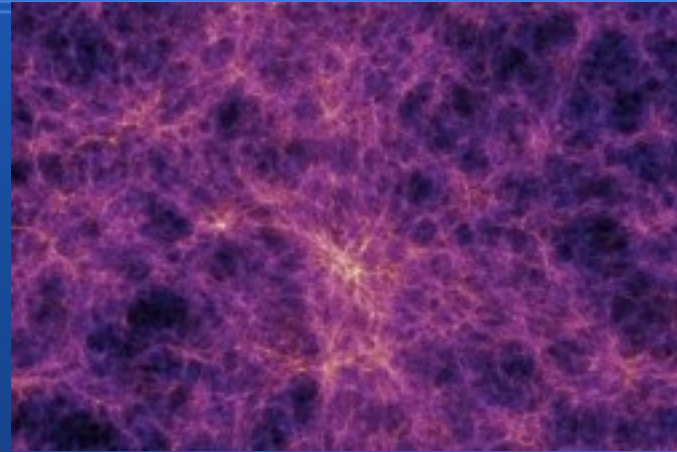
- Cubic Volume of  $500 h^{-1}$  Mpc of side.
- $10^9$  dark matter particles.
- $1.7 \times 10^{10} h^{-1} M_{\odot}$  mass resolution.
- Cosmological parameters:  
 $\Omega_m=0.25, \Omega_b=0.045, \Omega_{\Lambda}=0.75, h=0.73, \sigma_8=0.9, n=1.$
- Running time: a couple of months in a fully dedicated super-computing cluster.



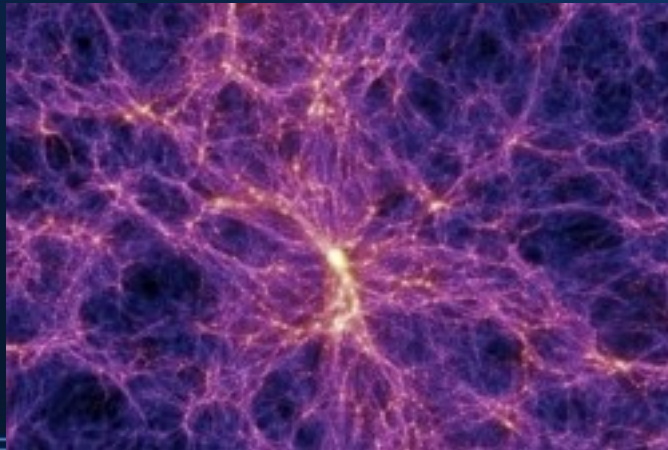
# N-body cosmological numerical simulation: The Millennium Run



$Z = 18.3$



$Z = 5.7$



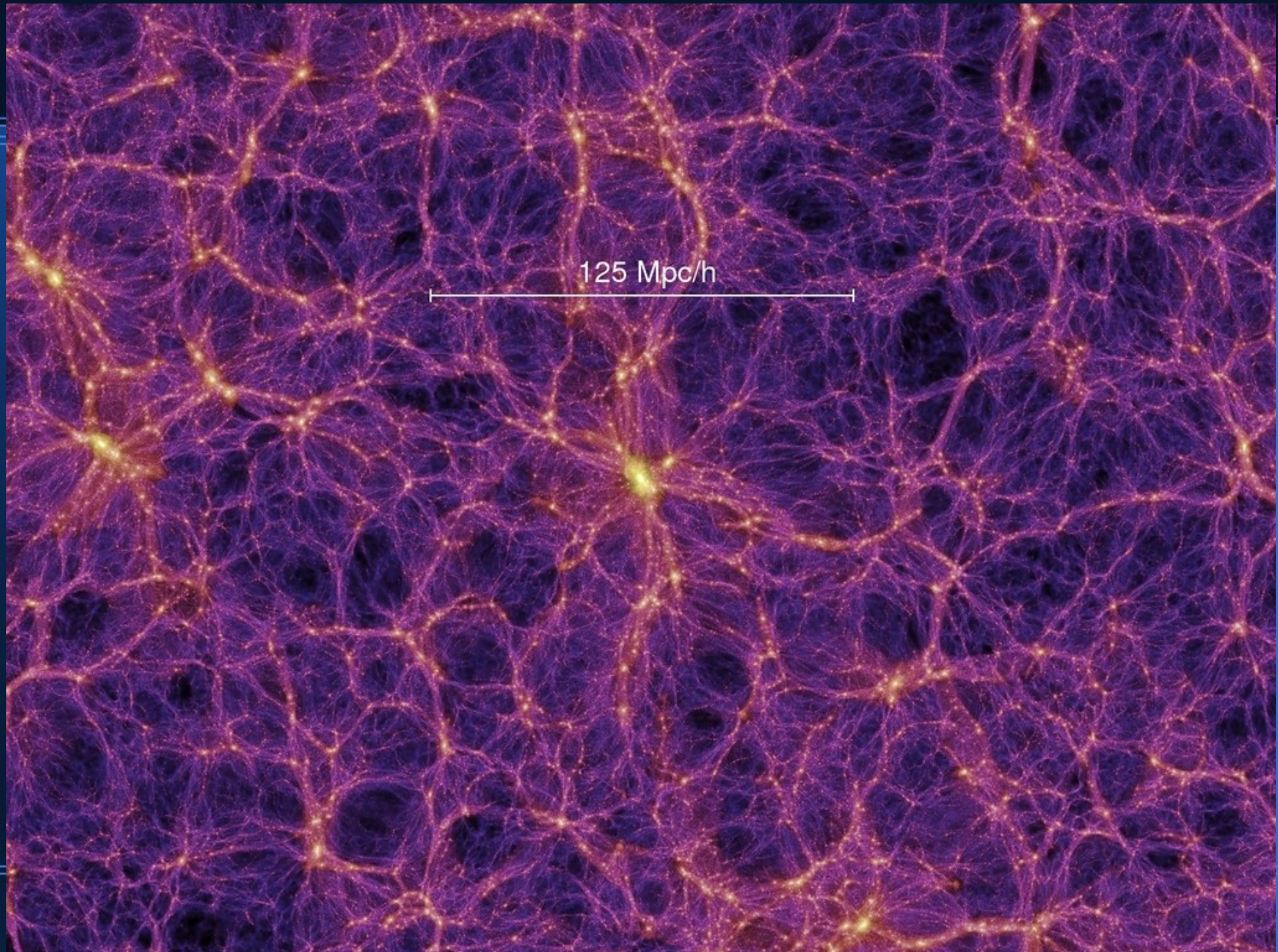
$Z = 1.4$



$Z = 0$

# The Millennium Run

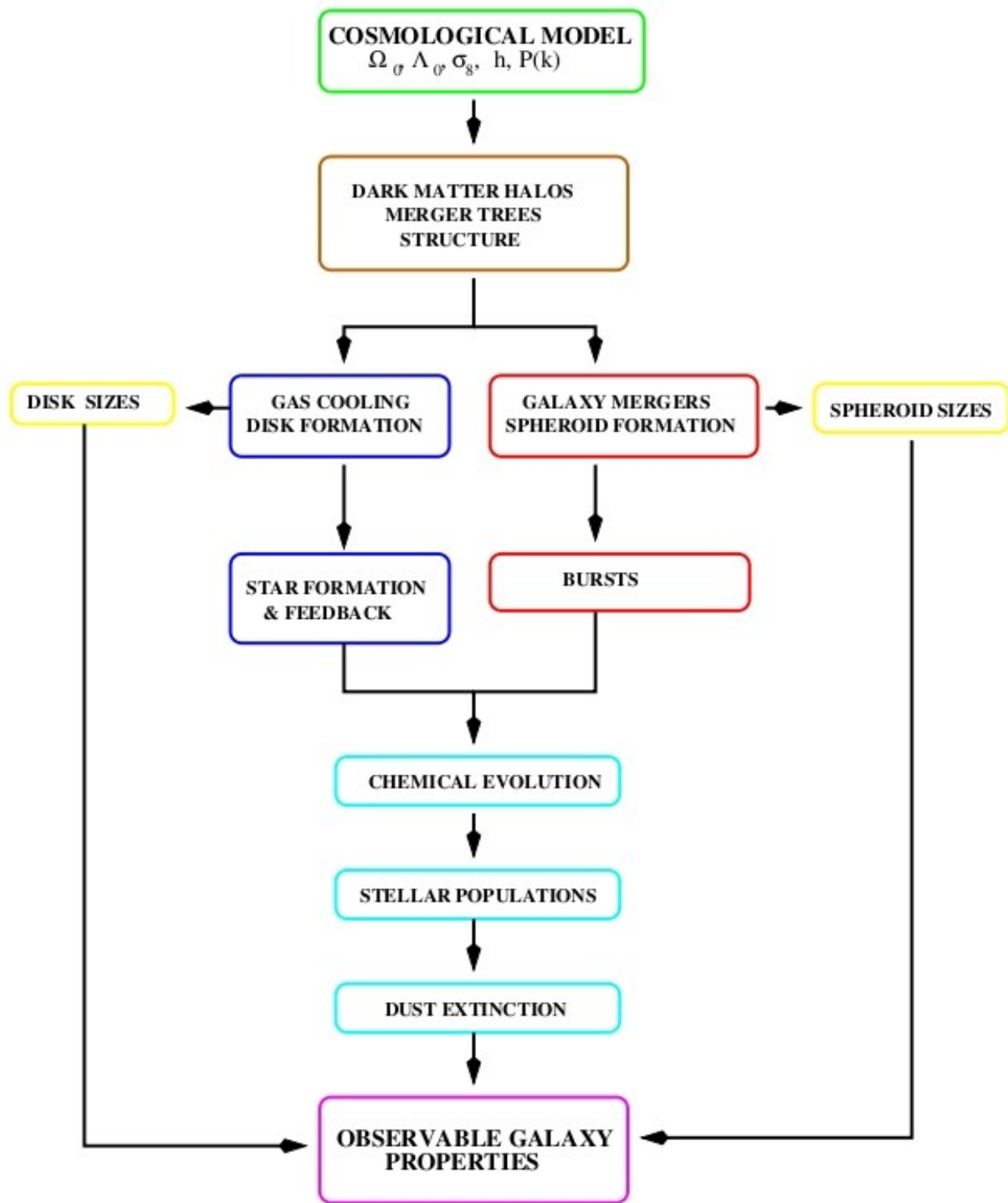
$z = 0$



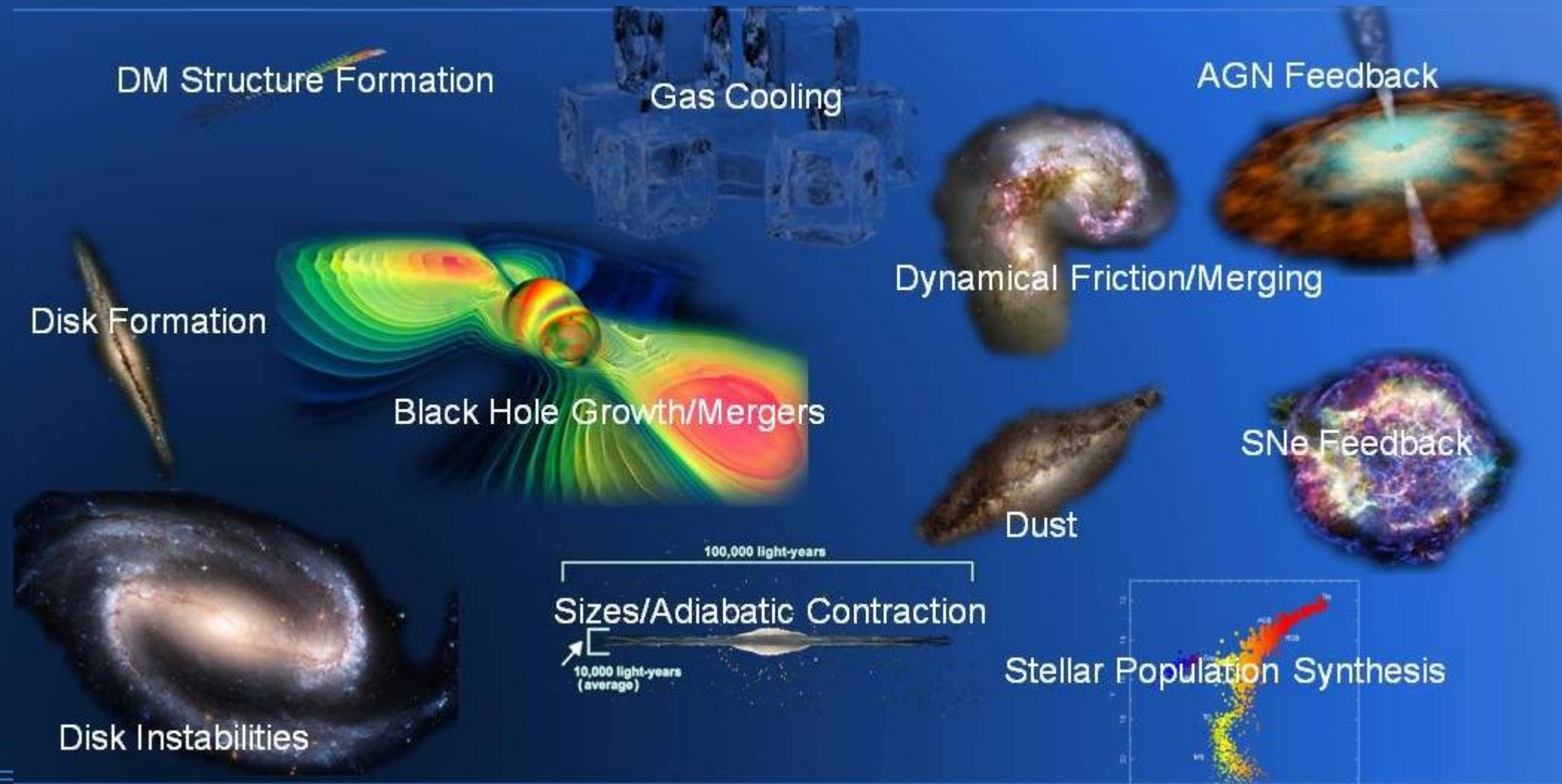


# How to build semianalytical galaxies?

## The semianalytical model of galaxy formation



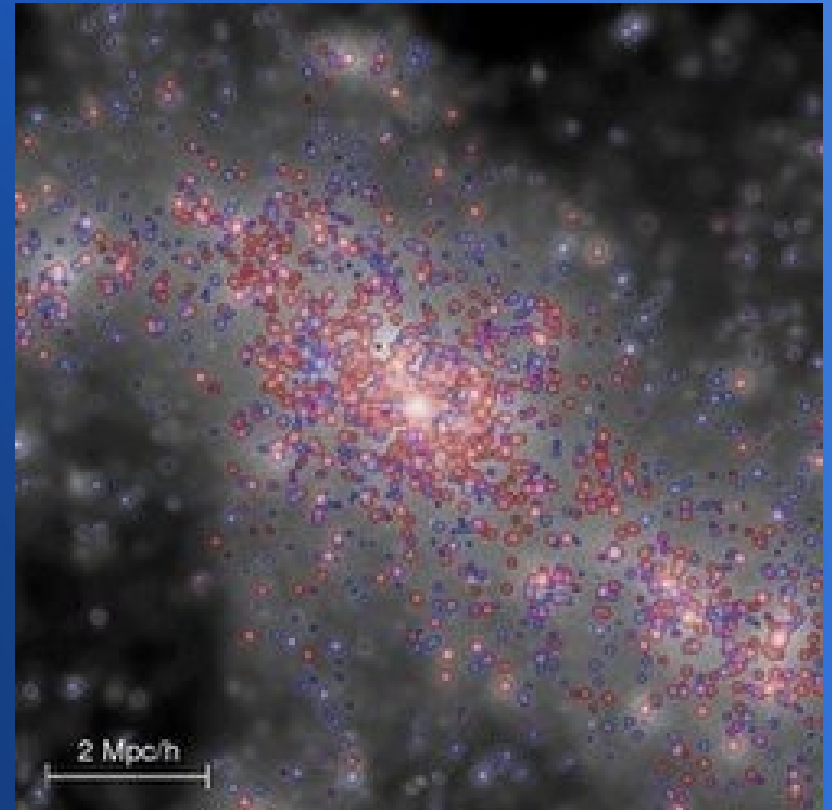
# The semianalytical model of galaxy formation



# The semianalytical model on top of the Millennium Simulation



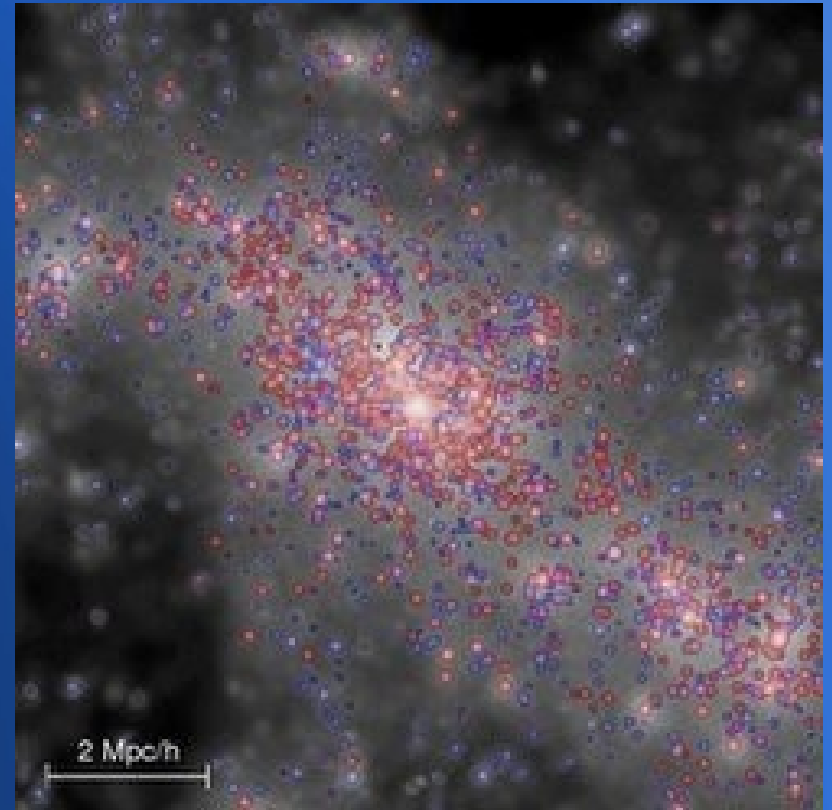
**Dark Matter**



**Galaxies**

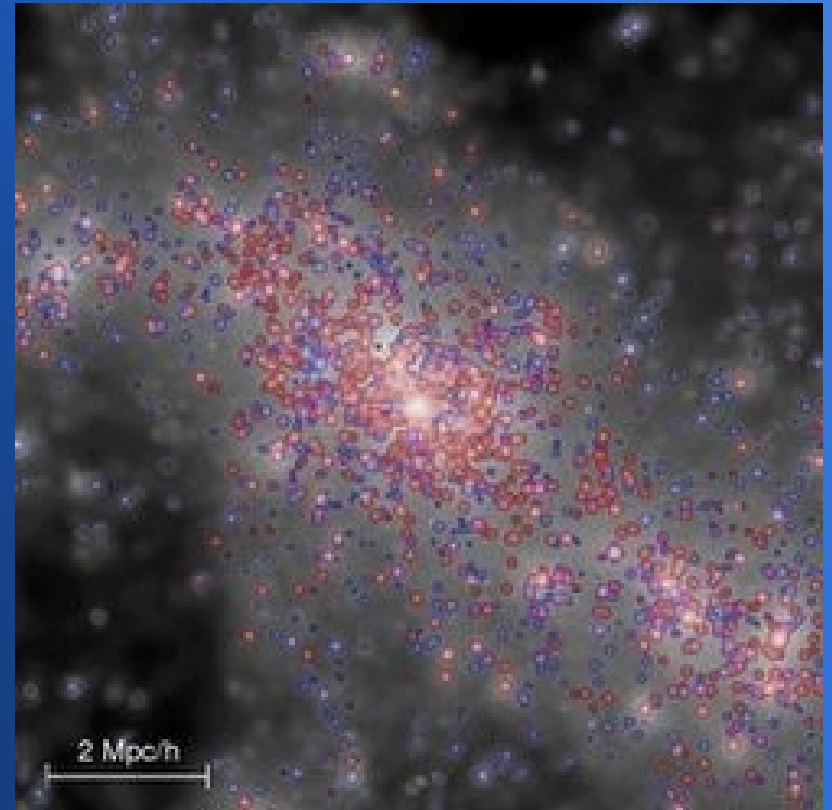
# The semianalytical model on top of the Millennium Simulation

- Croton et al (2006)
- Bower et al. (2006)
- De Lucia et al. (2007)
- Bertone et al. (2007)
- Guo et al. (2011)



# The semianalytical model on top of the Millennium Simulation

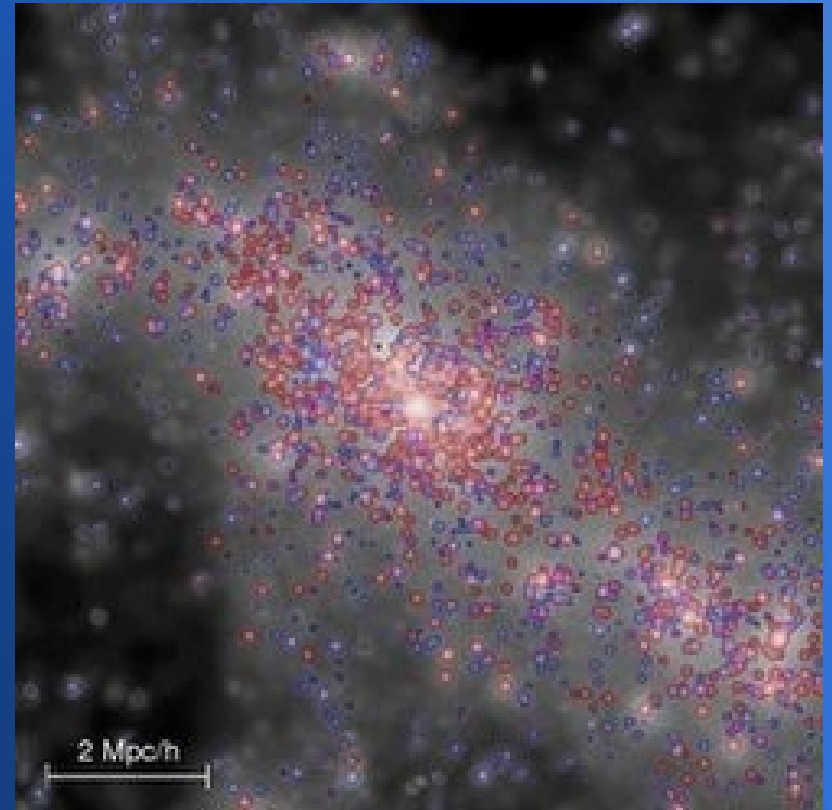
- Croton et al (2006)
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- Bertone et al. (2007)
- Guo et al. (2011)



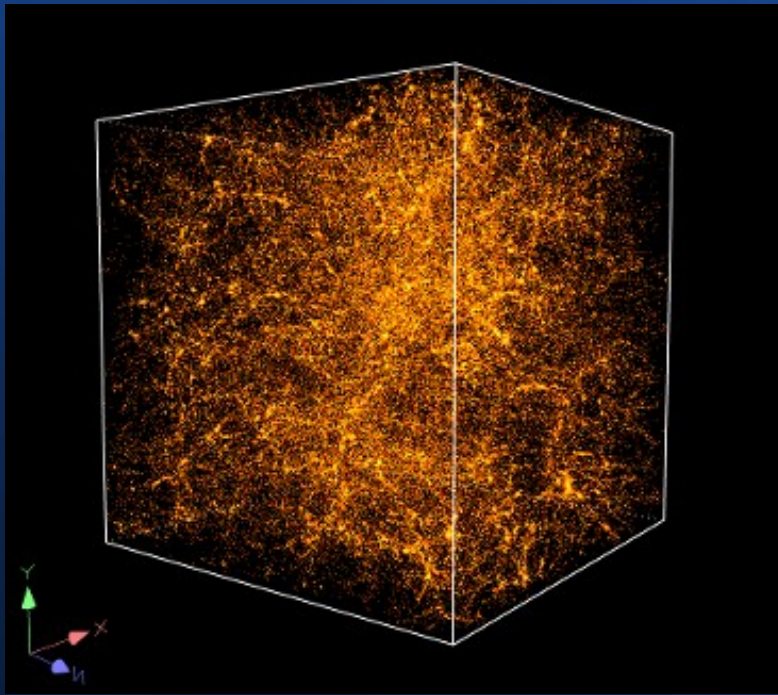
# The semianalytical model on top of the Millennium Simulation

Guo et al. (2011)

- Increased the efficiency of supernova feedback.
- More realistic satellite galaxy evolution and mergers.
- Tidal disruption of satellite galaxies.

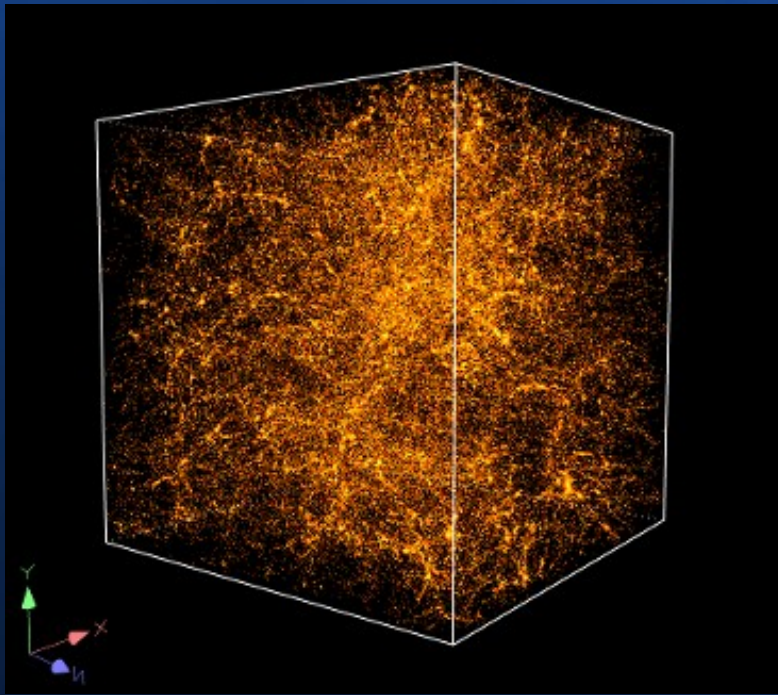


# Reaching the survey deep

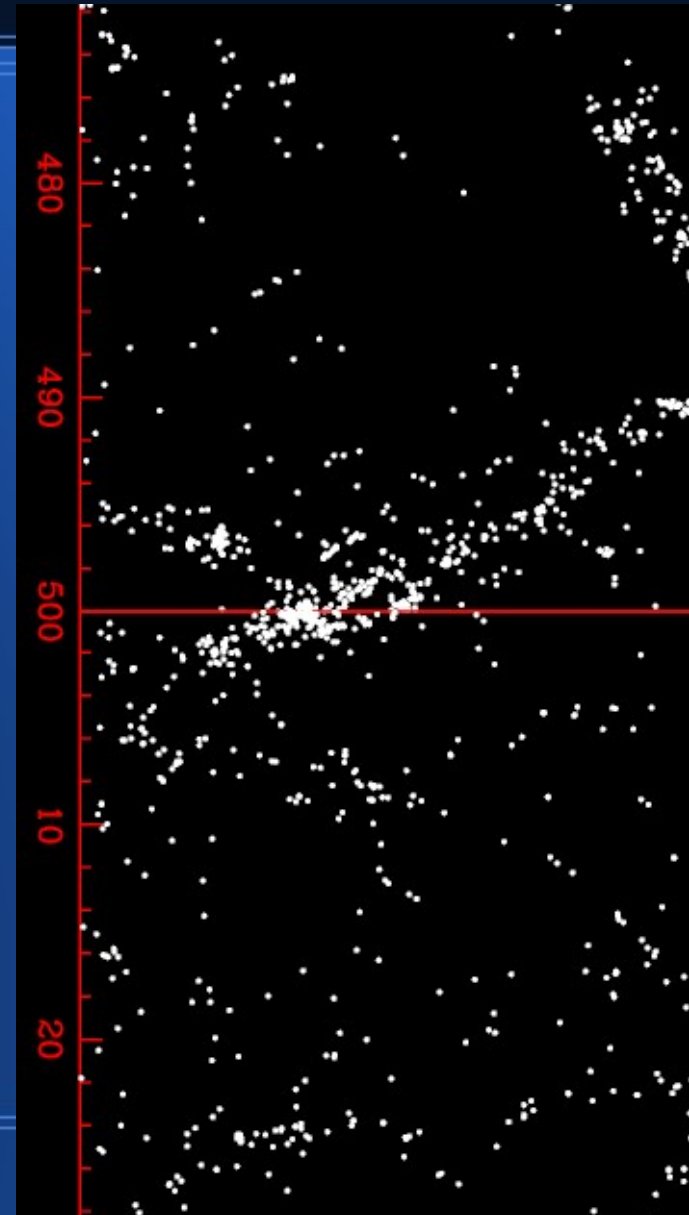


**$500 h^{-1} \text{ Mpc}$**

# Stacking cubes to reach the survey deep

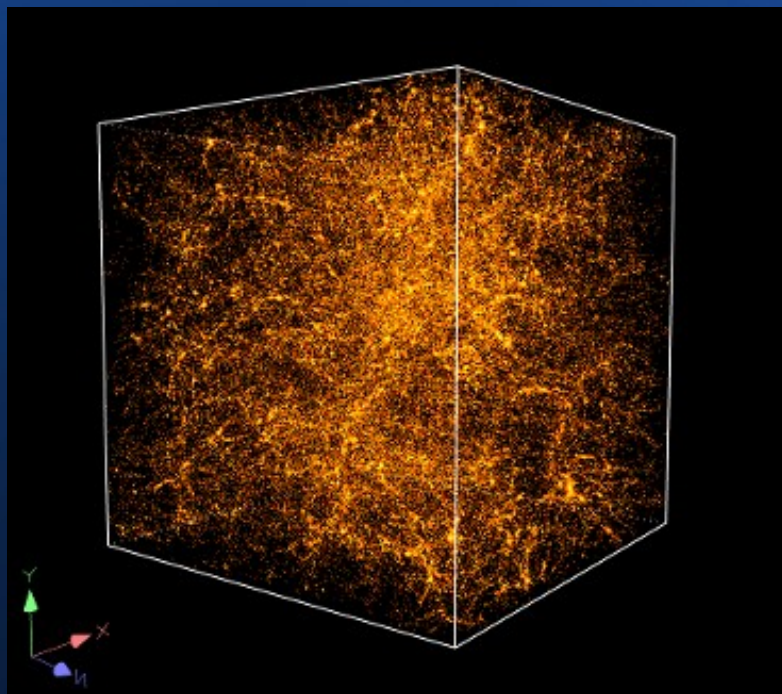


**Periodic box**

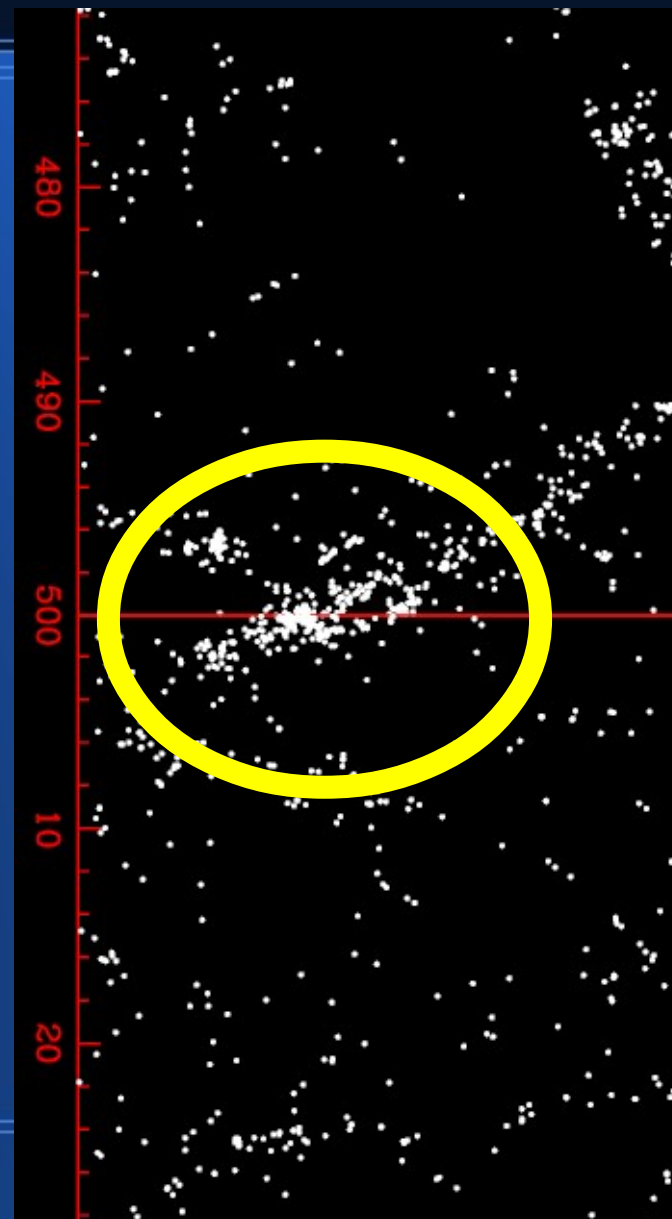




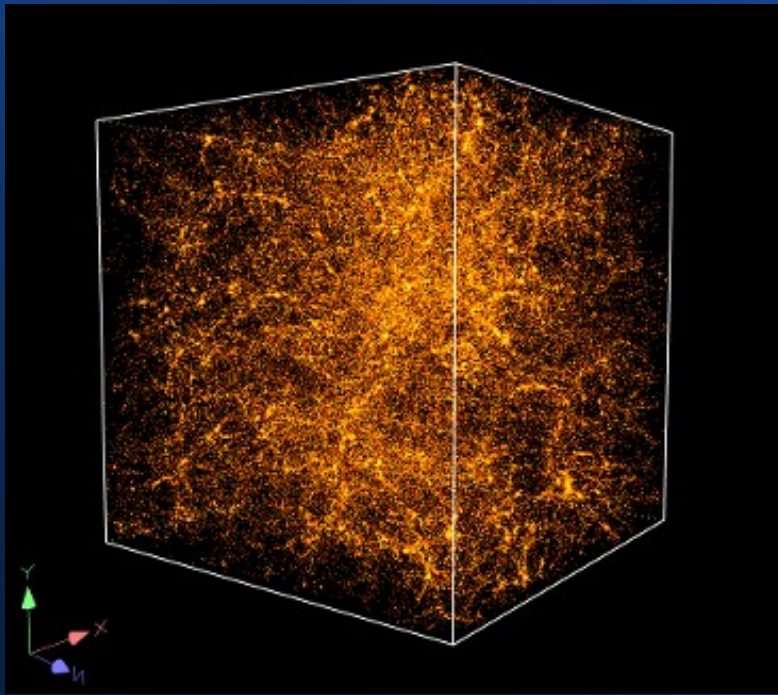
# Stacking cubes to reach the survey deep



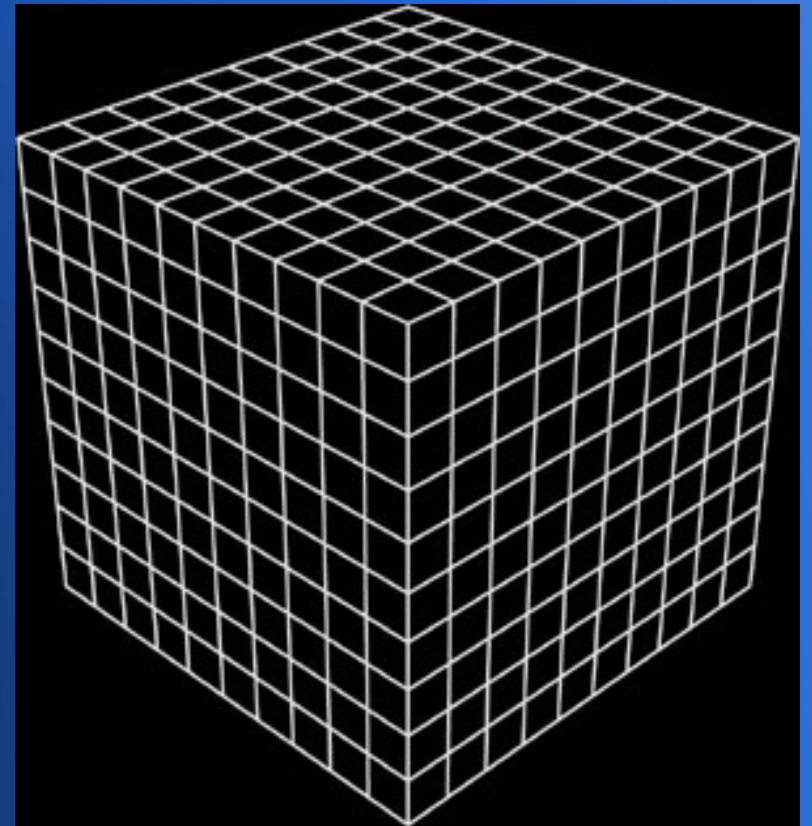
**Periodic box**



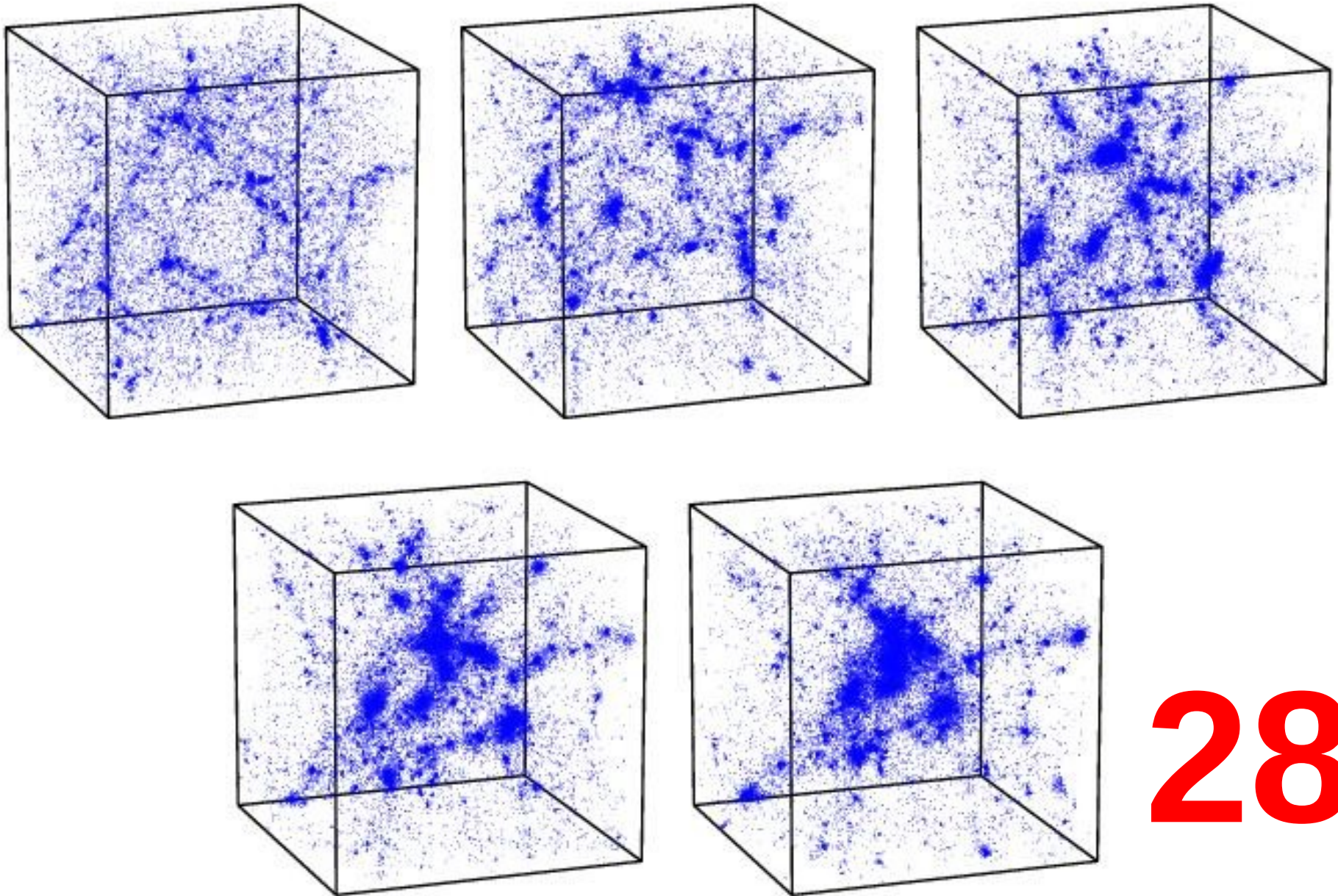
# Stacking cubes to reach the survey deep



**Periodic box**

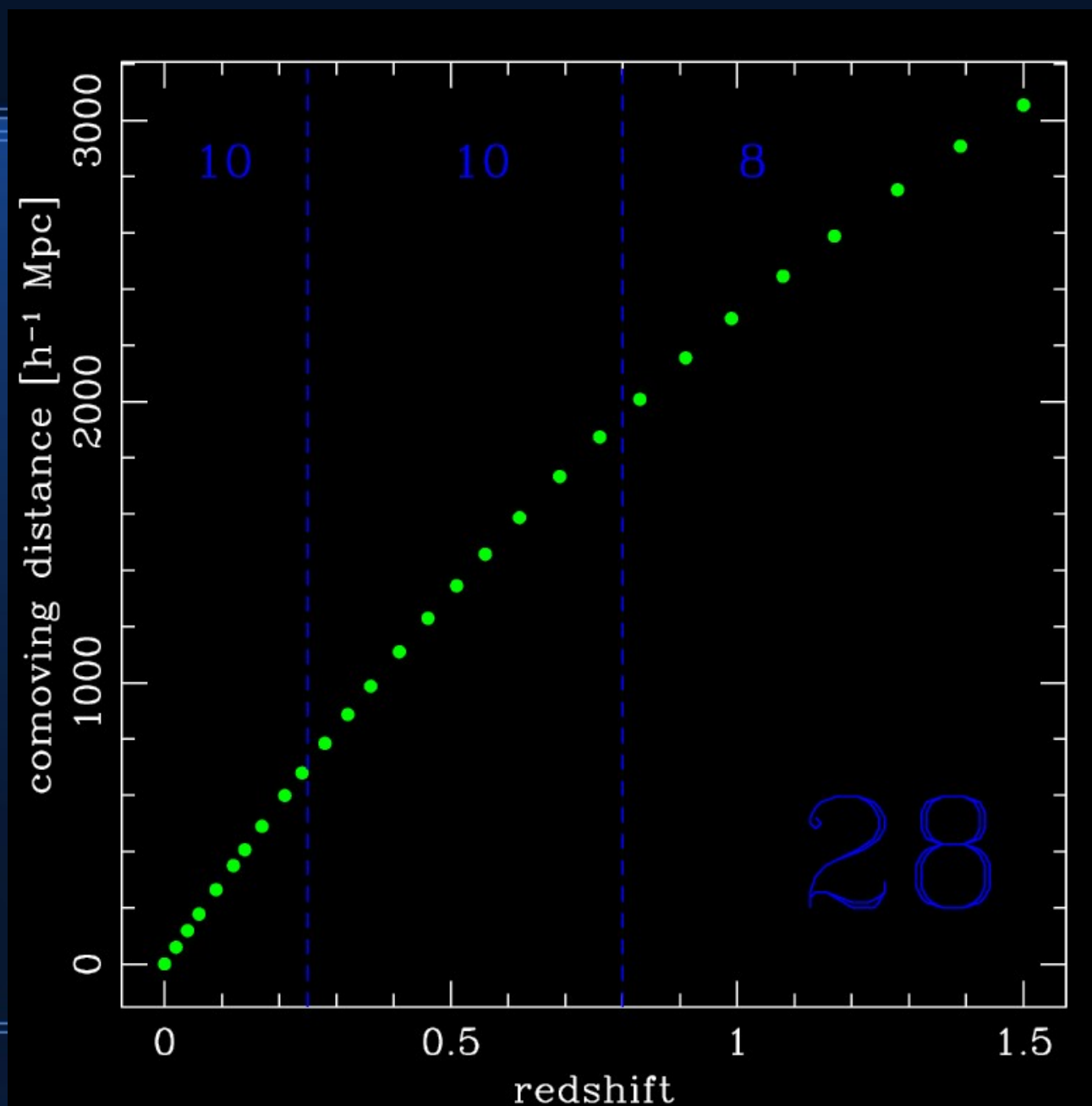


# Using different snapshots from the simulation

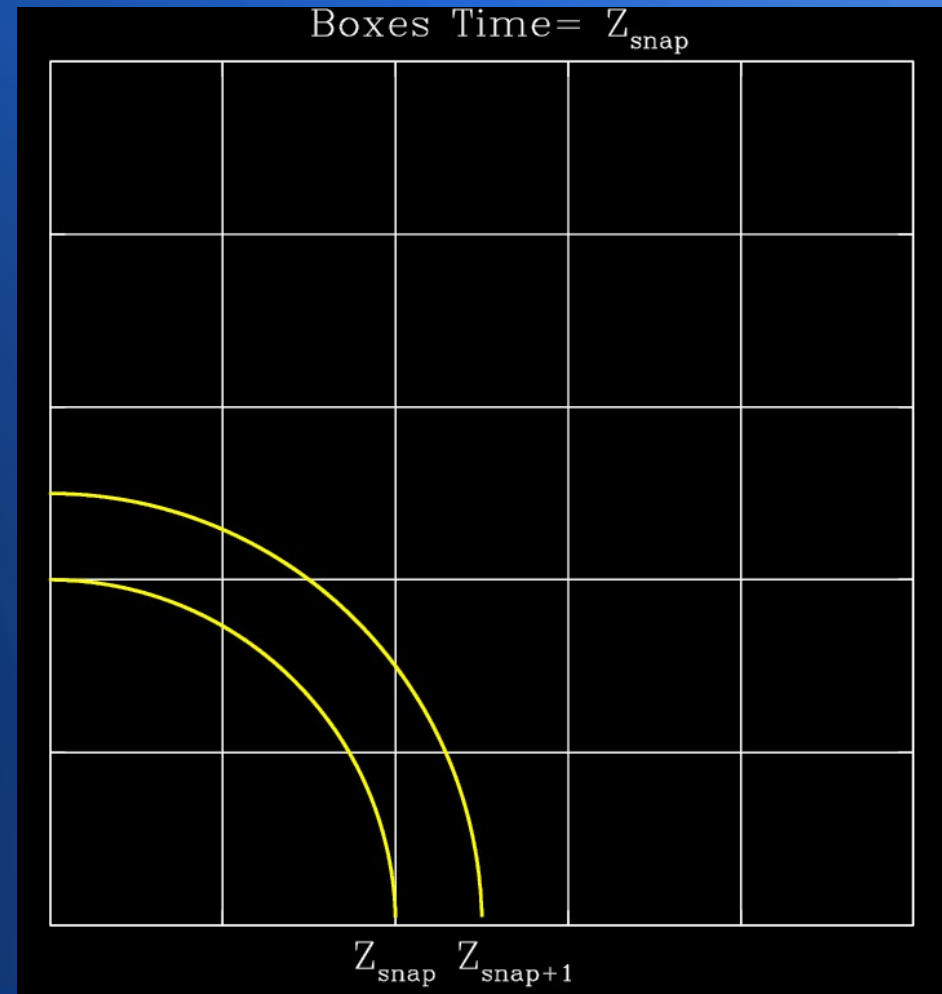
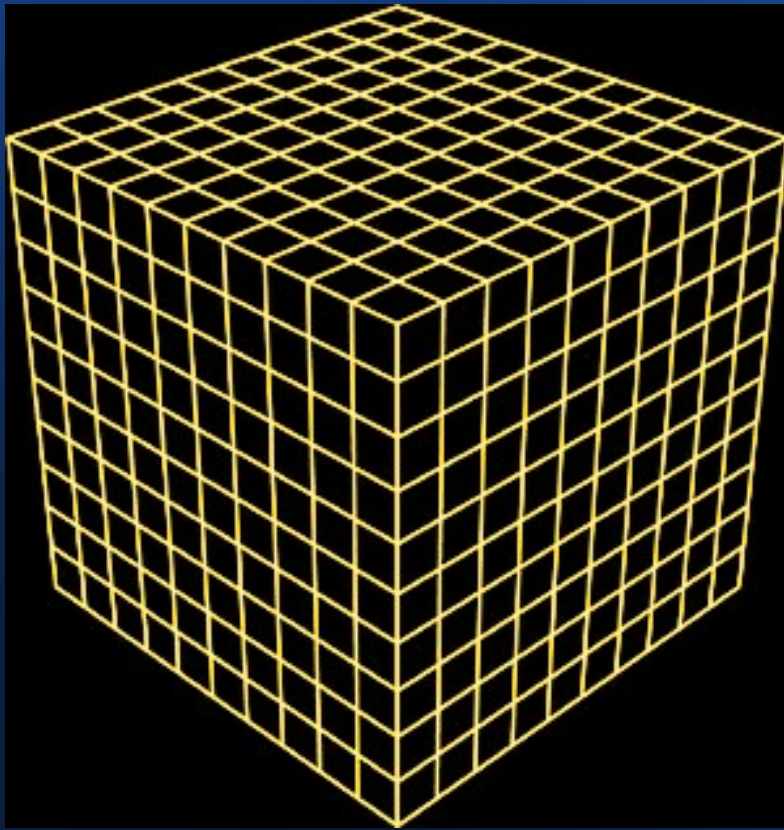


**28**

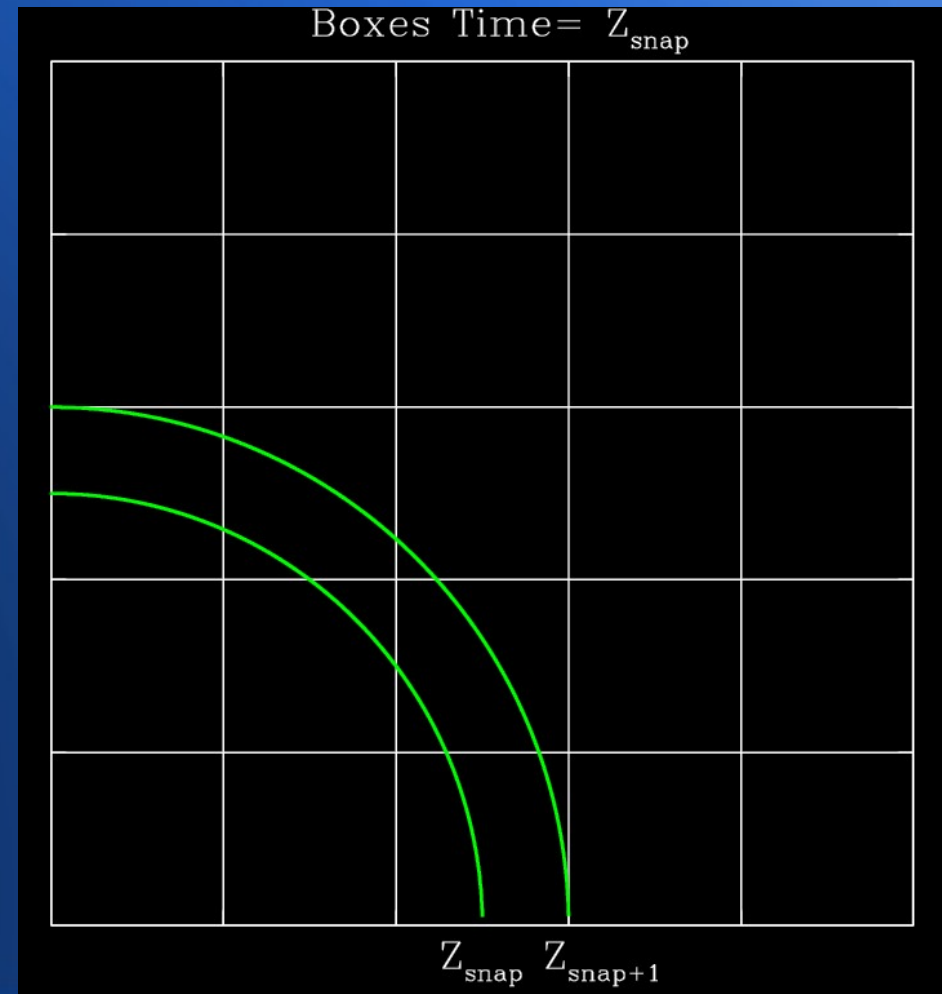
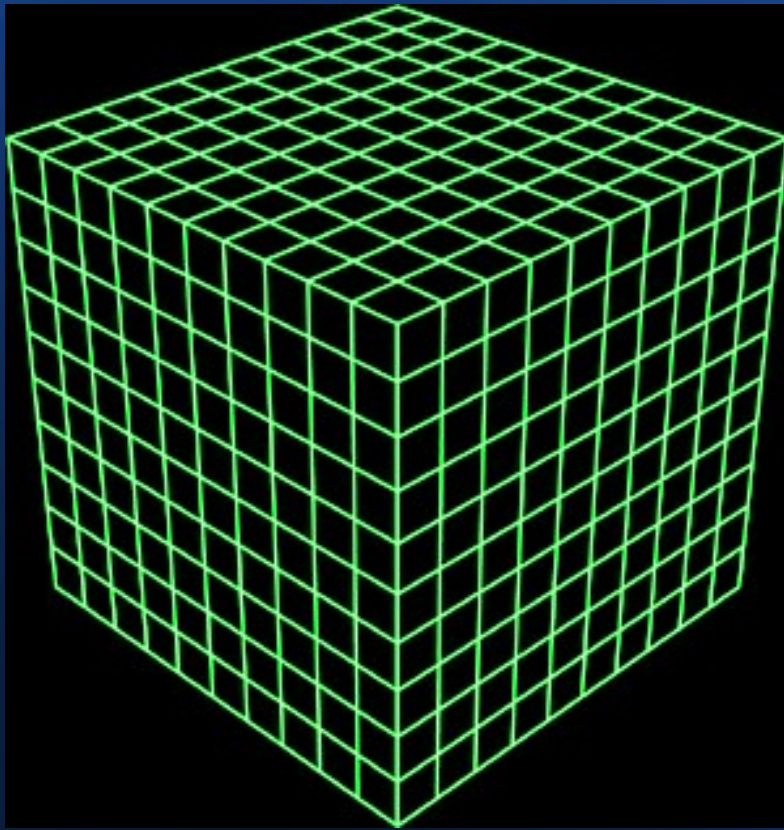
# Using different snapshots from the simulation



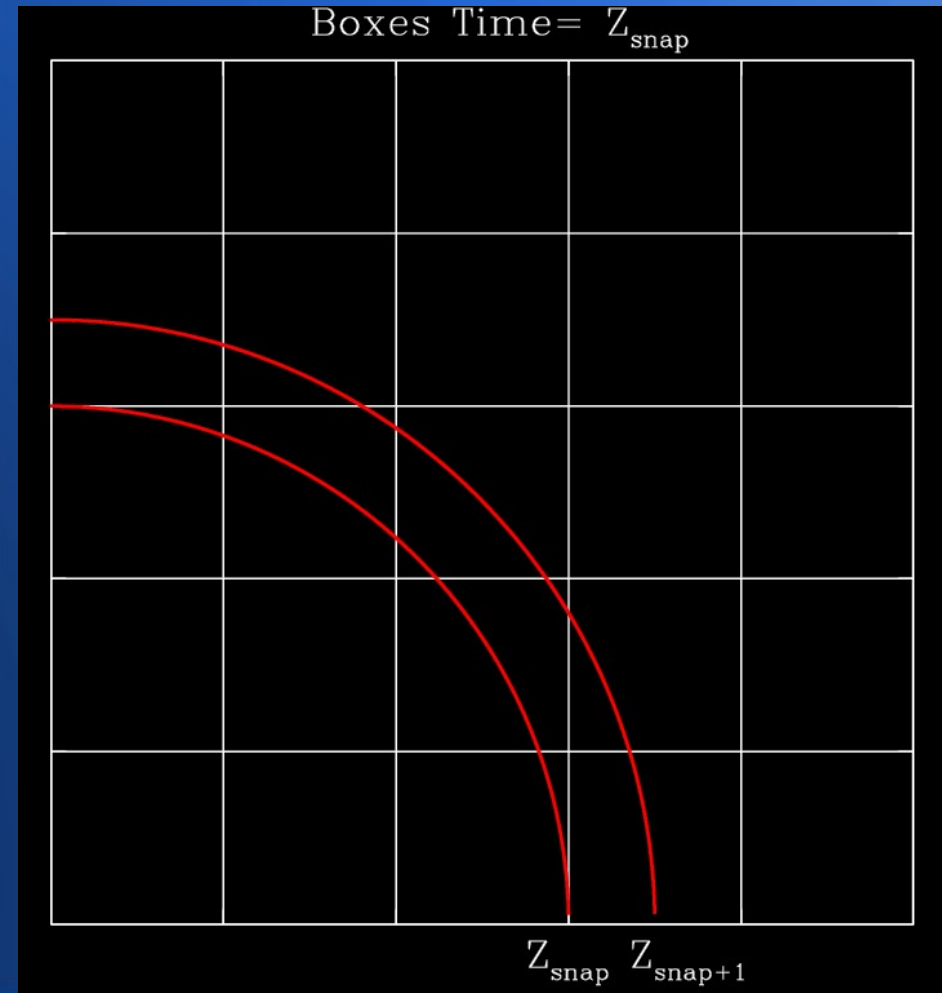
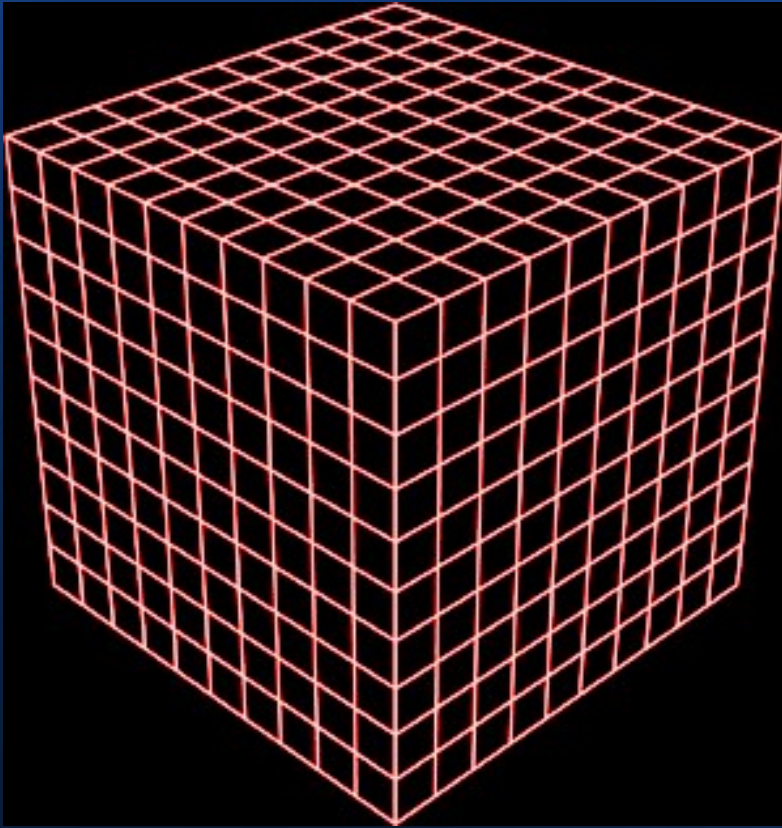
# Extracting the strips from different times



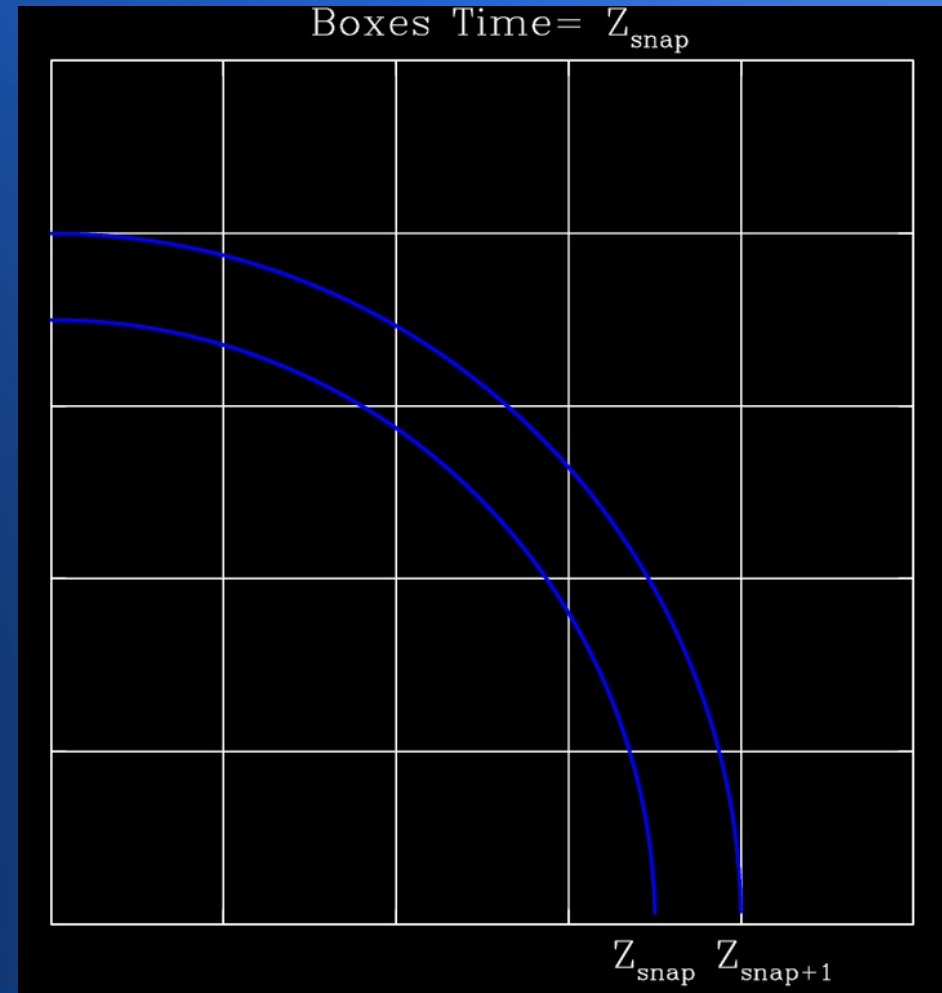
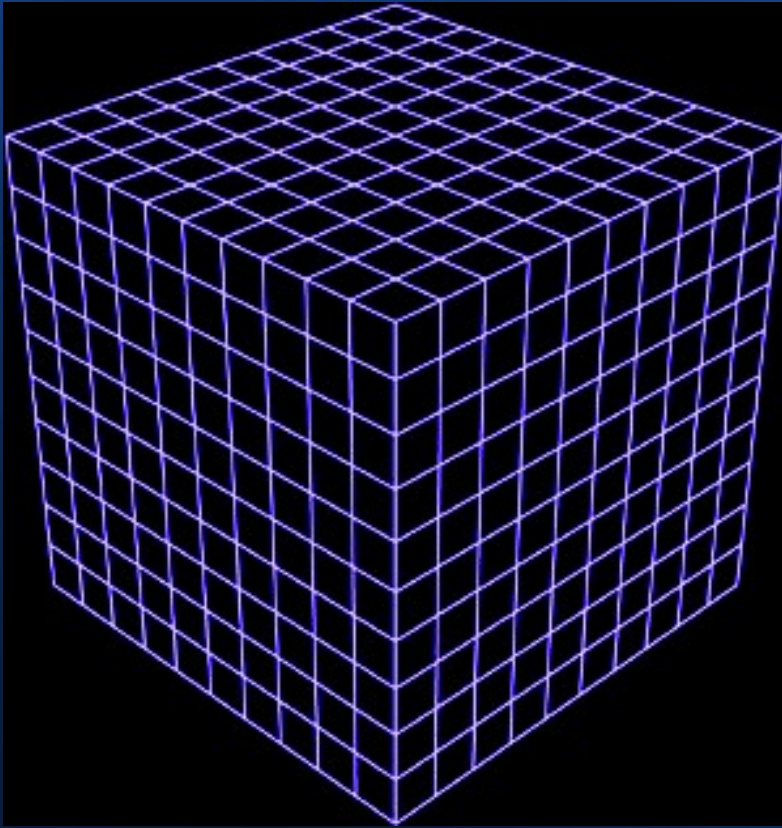
# Extracting the strips from different times



# Extracting the strips from different times

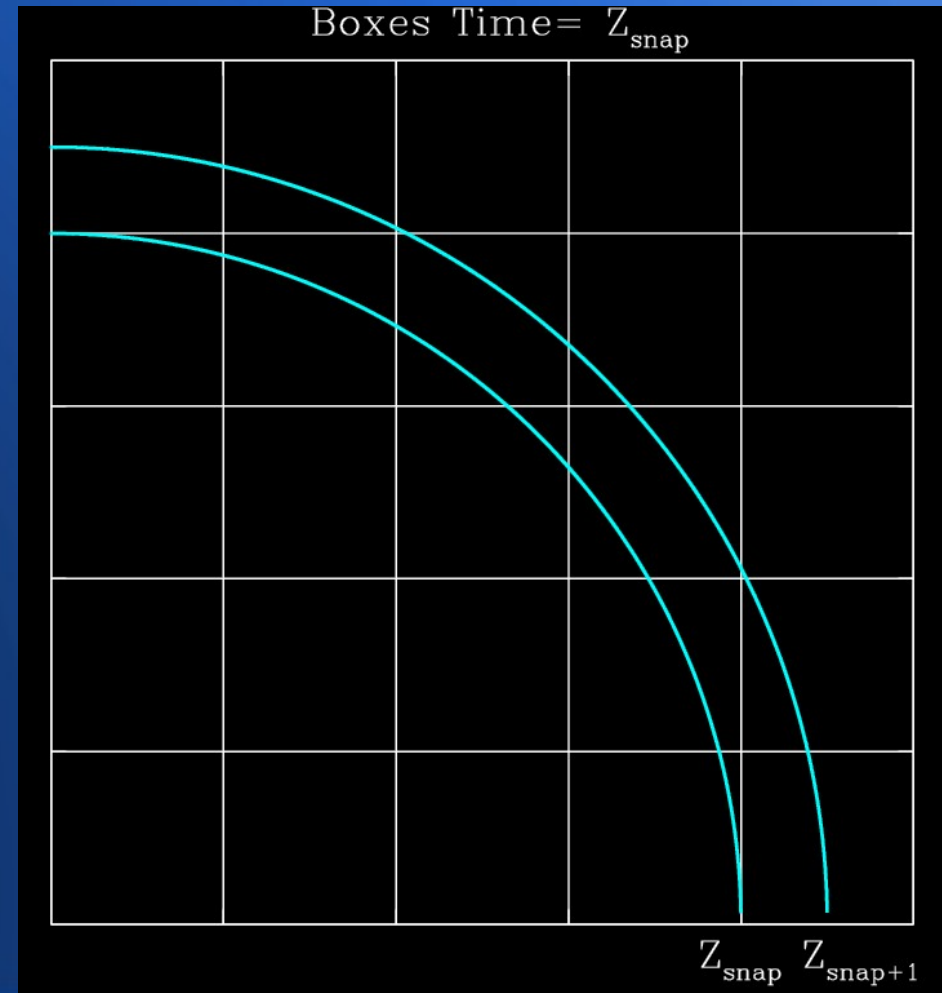
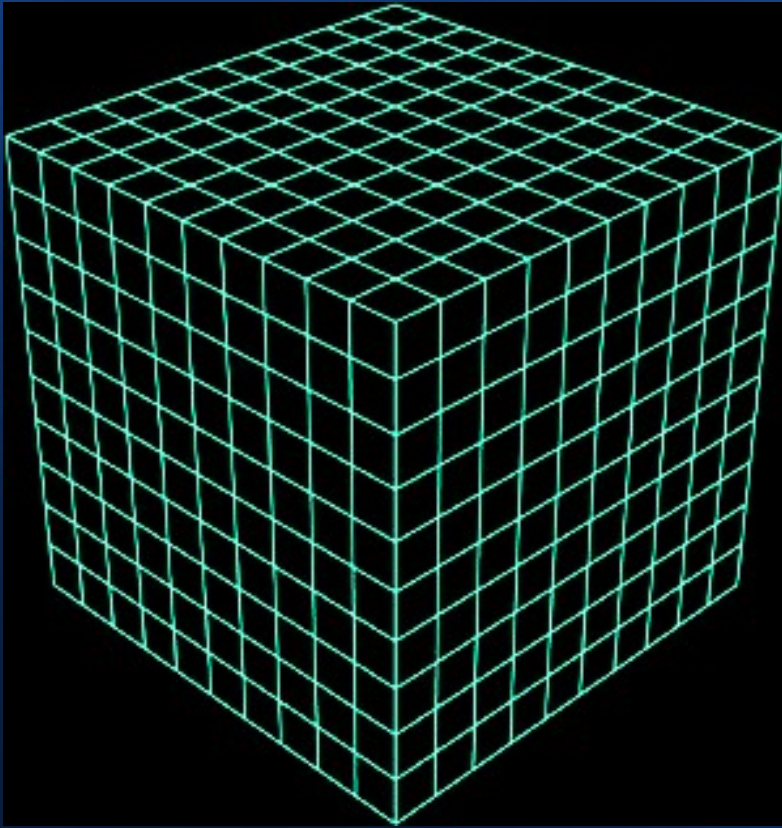


# Extracting the strips from different times

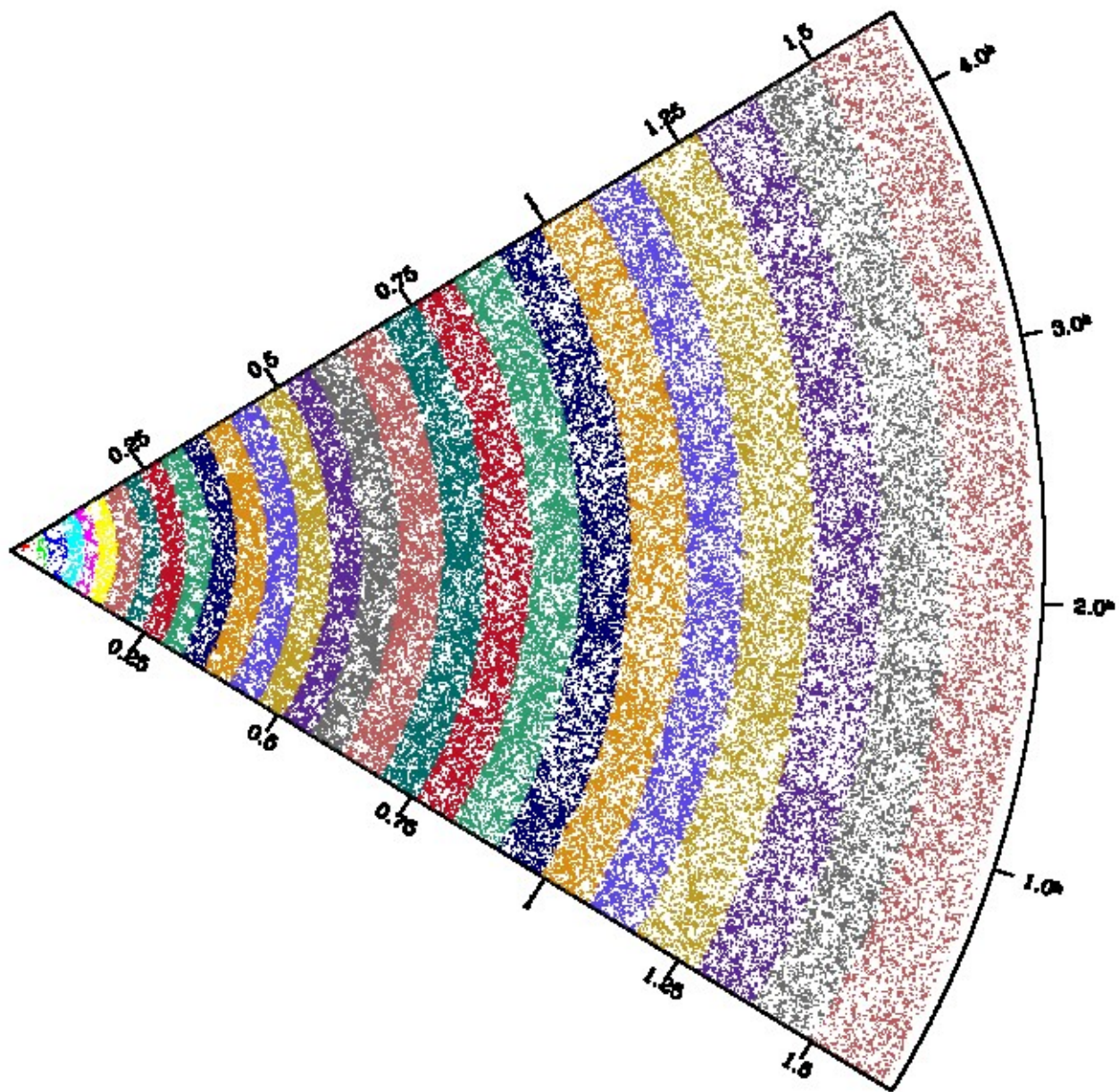




# Extracting the strips from different times



# Constructing the lightcone



# How to overcome the discreteness of the simulation snapshots?

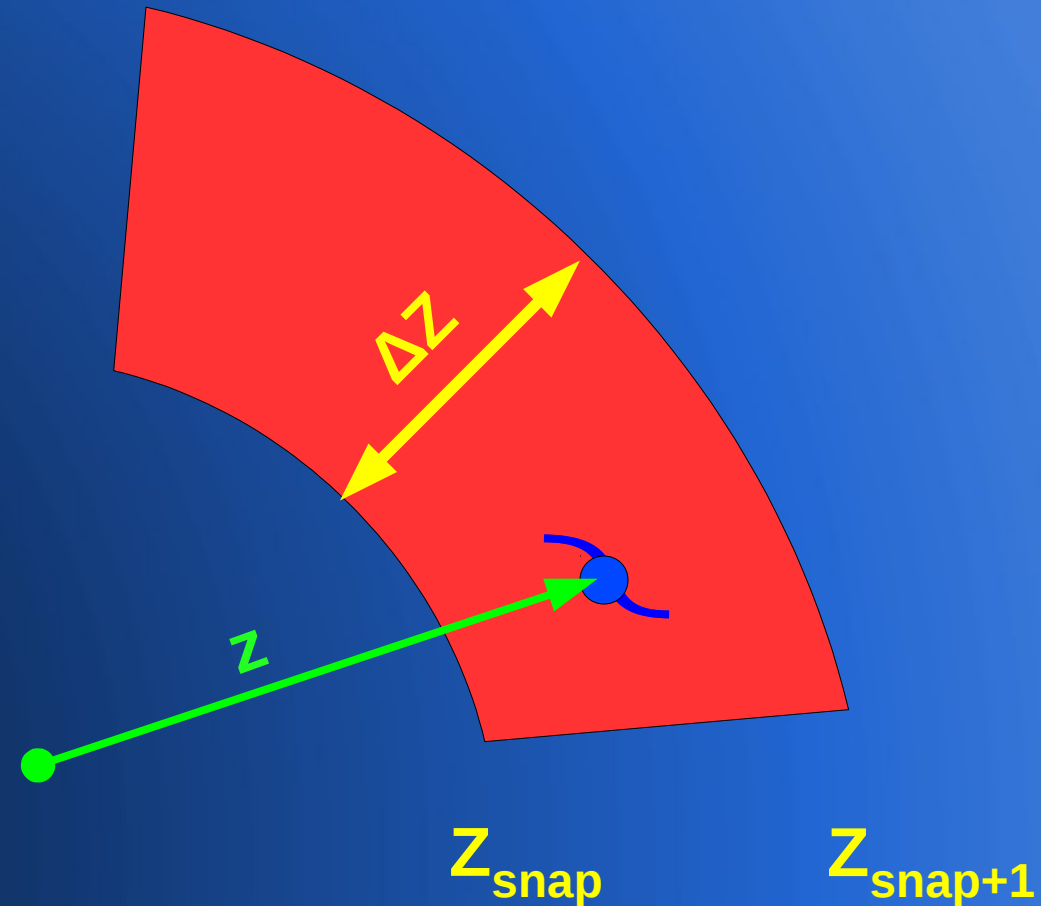
Interpolating positions, velocities and magnitudes:

$$\alpha = \frac{z - Z_{snap}}{Z_{snap+1} - Z_{snap}}$$

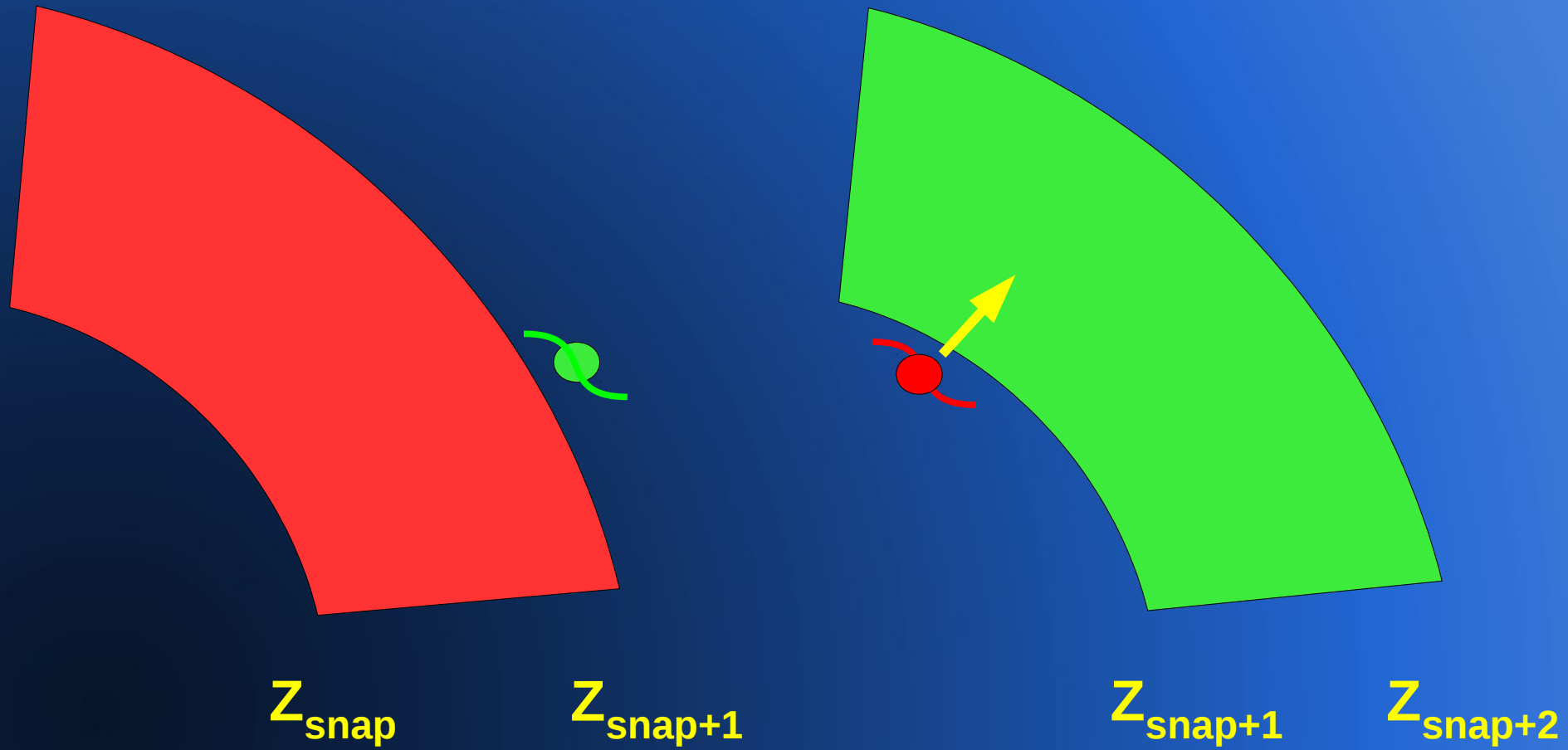
$$X = X_{snap} + \alpha (X_{snap+1} - X_{snap})$$

$$V = V_{snap} + \alpha (V_{snap+1} - V_{snap})$$

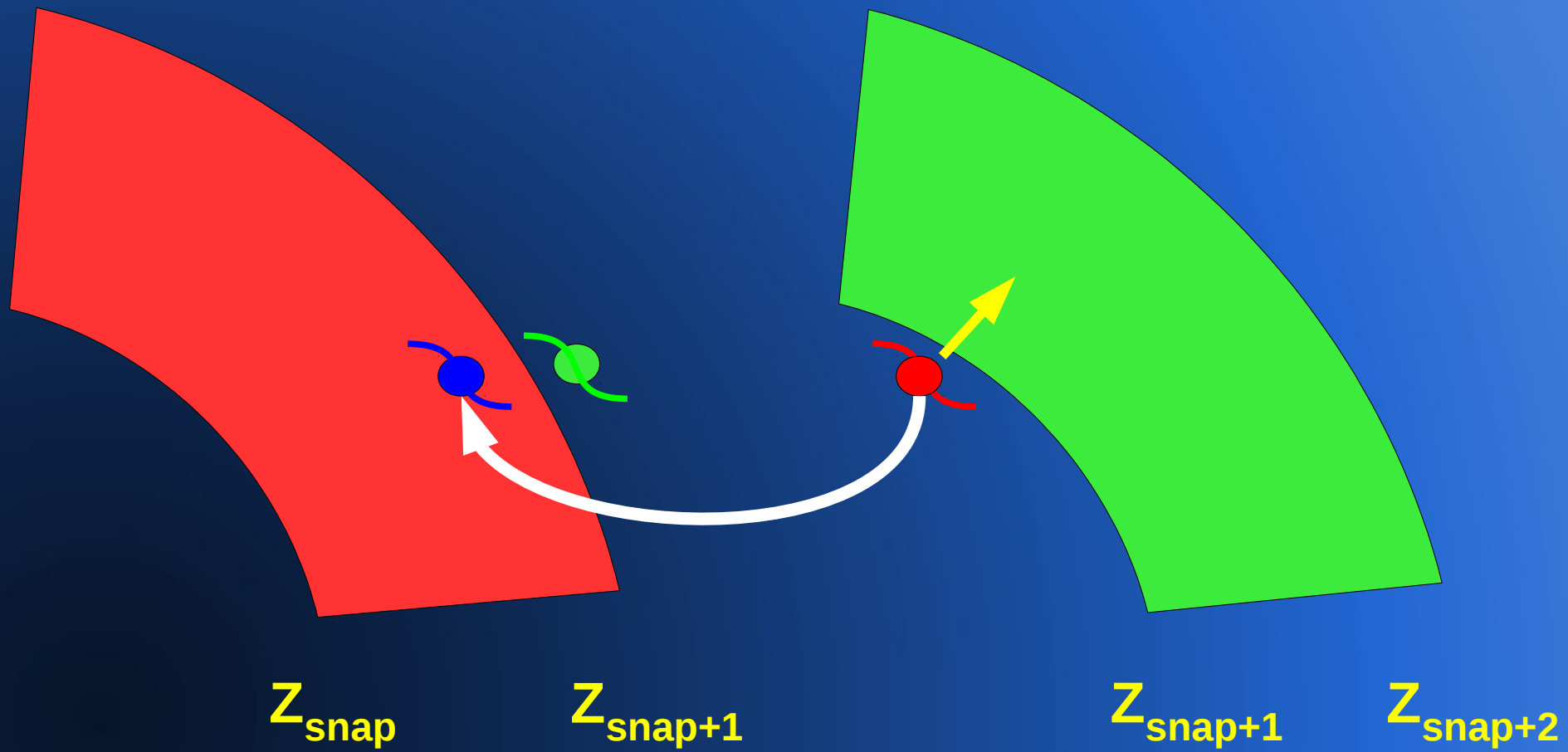
$$M = M_{snap} + \alpha (M_{snap+1} - M_{snap})$$



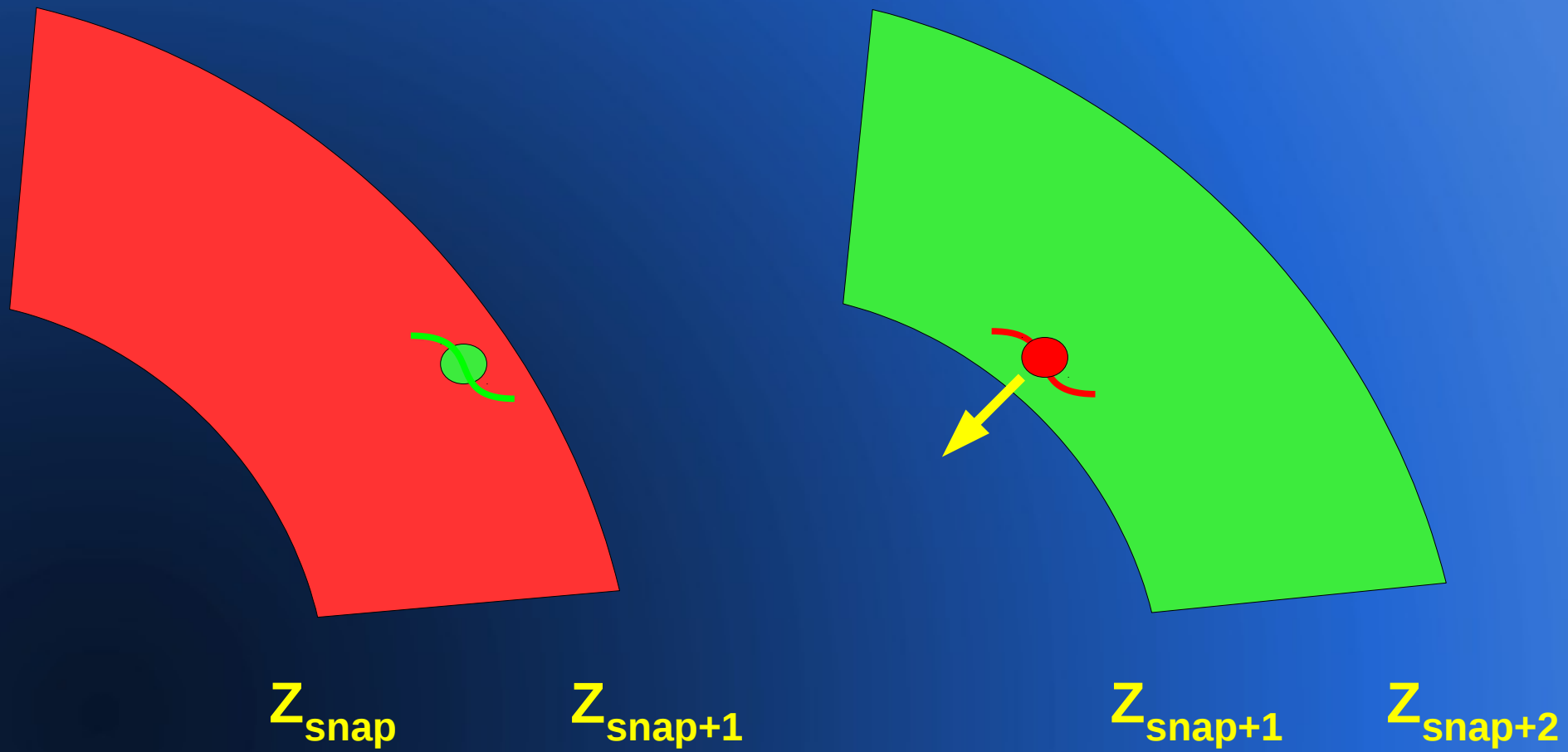
# The problem of missing galaxies



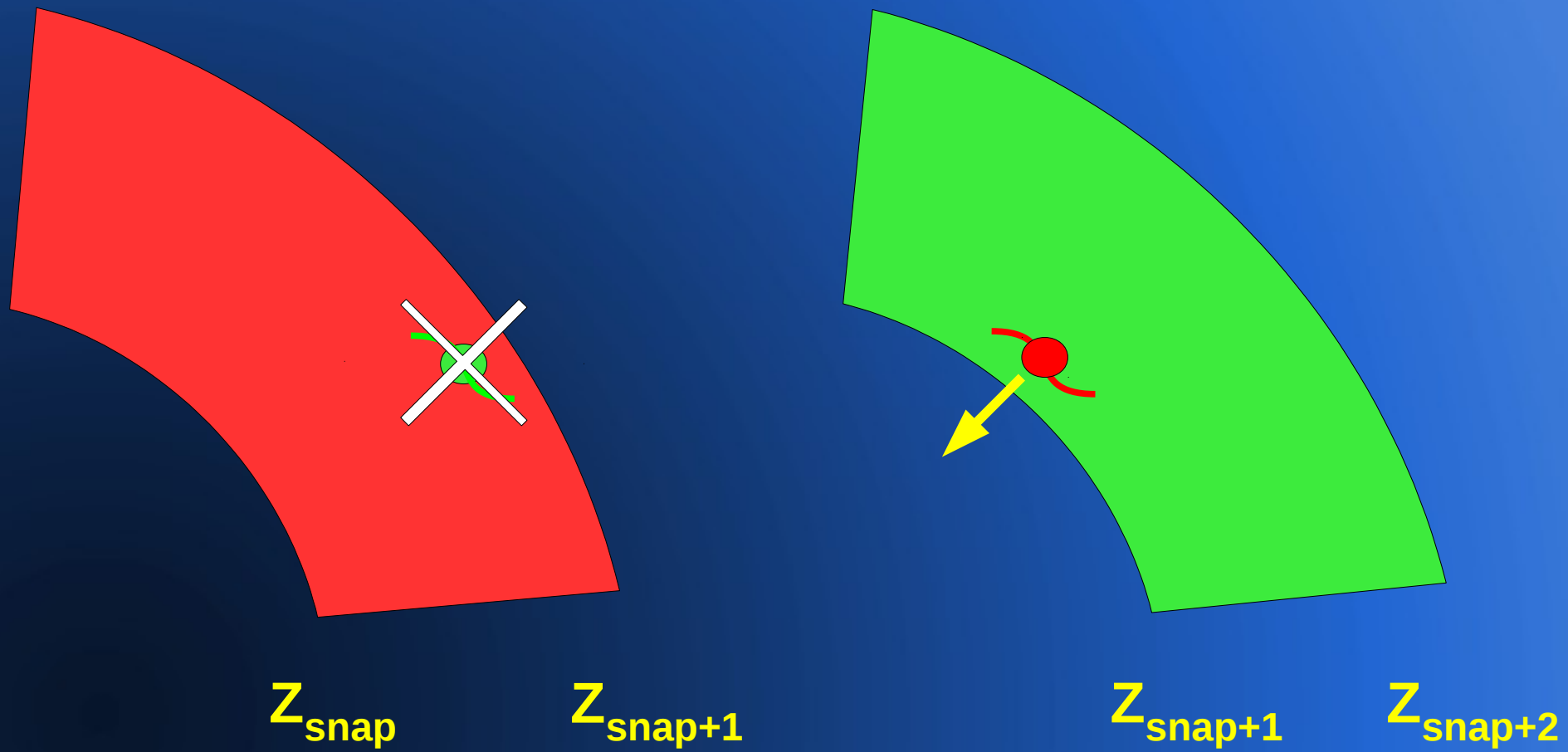
# The problem of missing galaxies



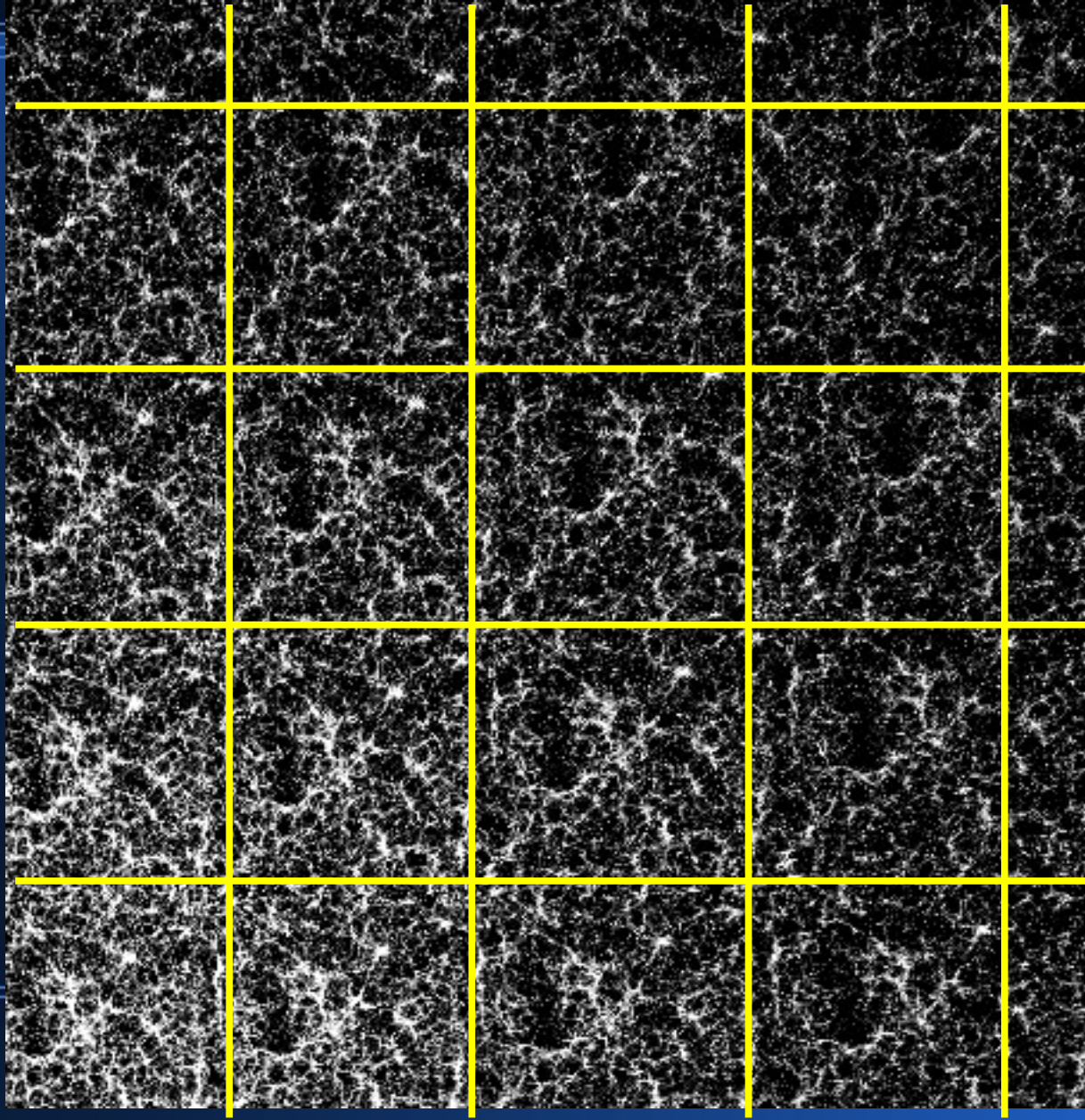
# The problem of repeated galaxies



# The problem of repeated galaxies

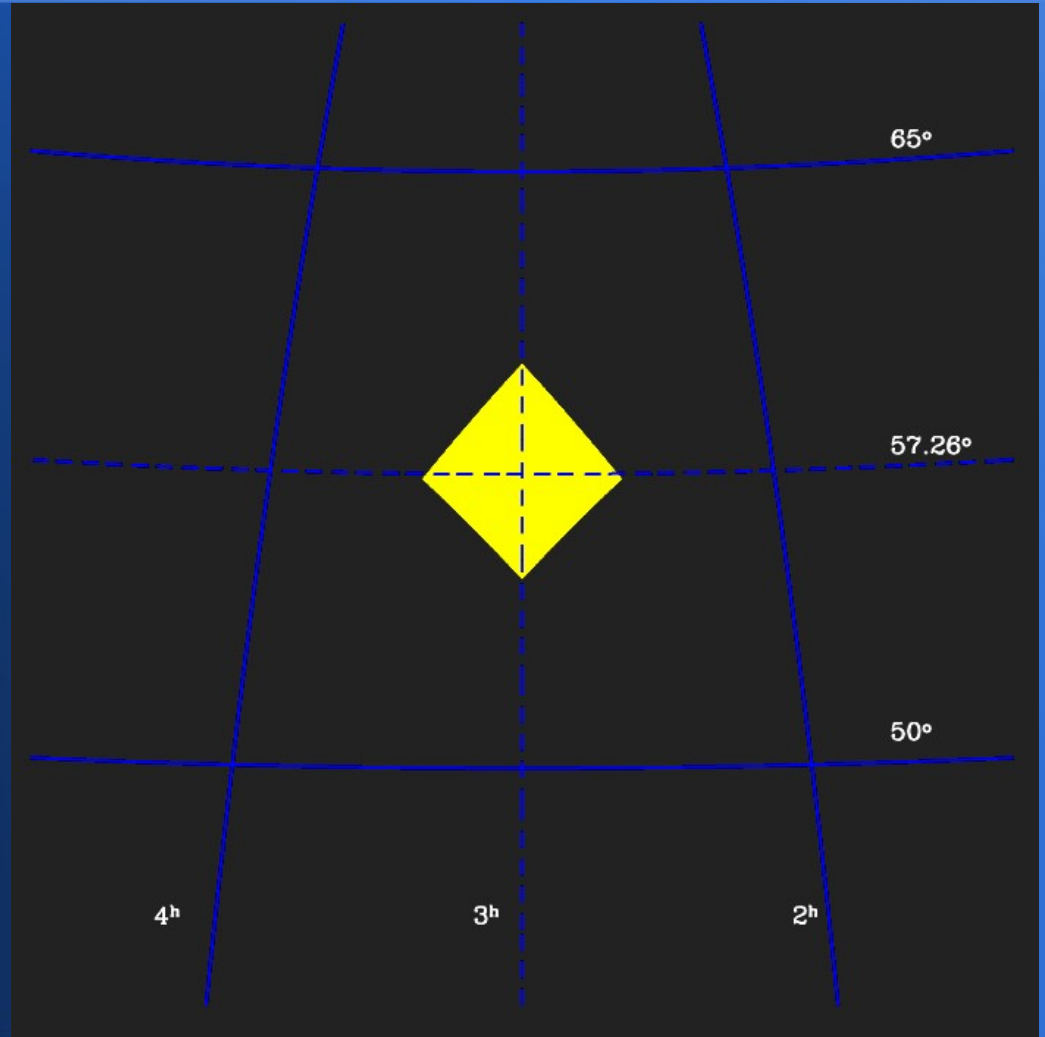
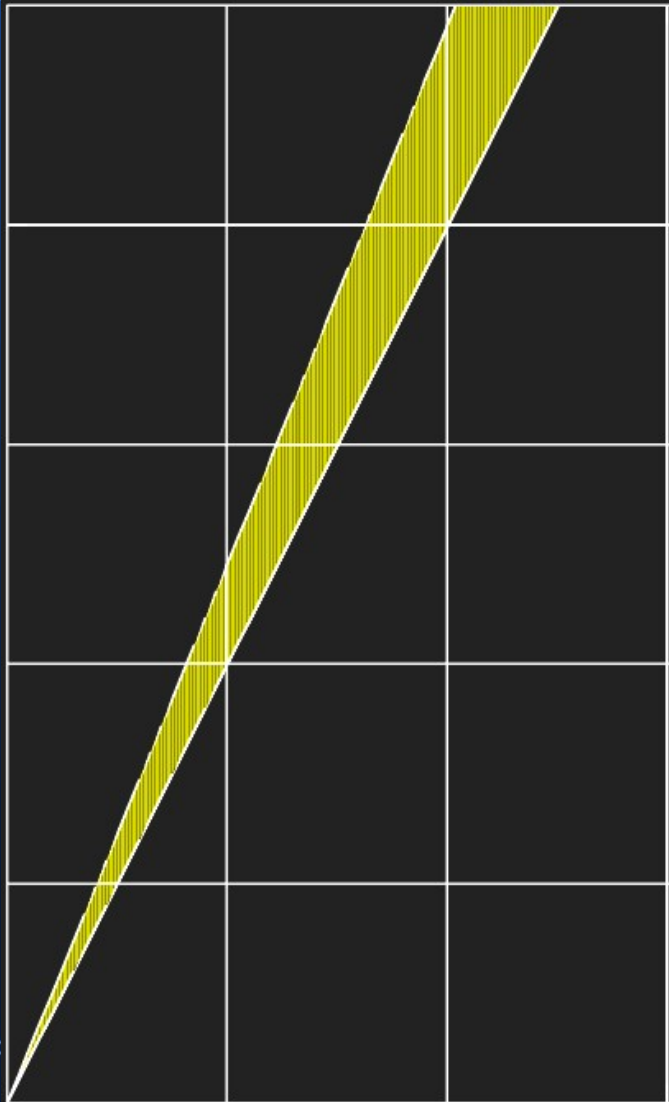


# How to overcome the repeated large structures due to the small size of the simulation box?





# How to overcome the repeated large structures due to the small size of the simulation box?

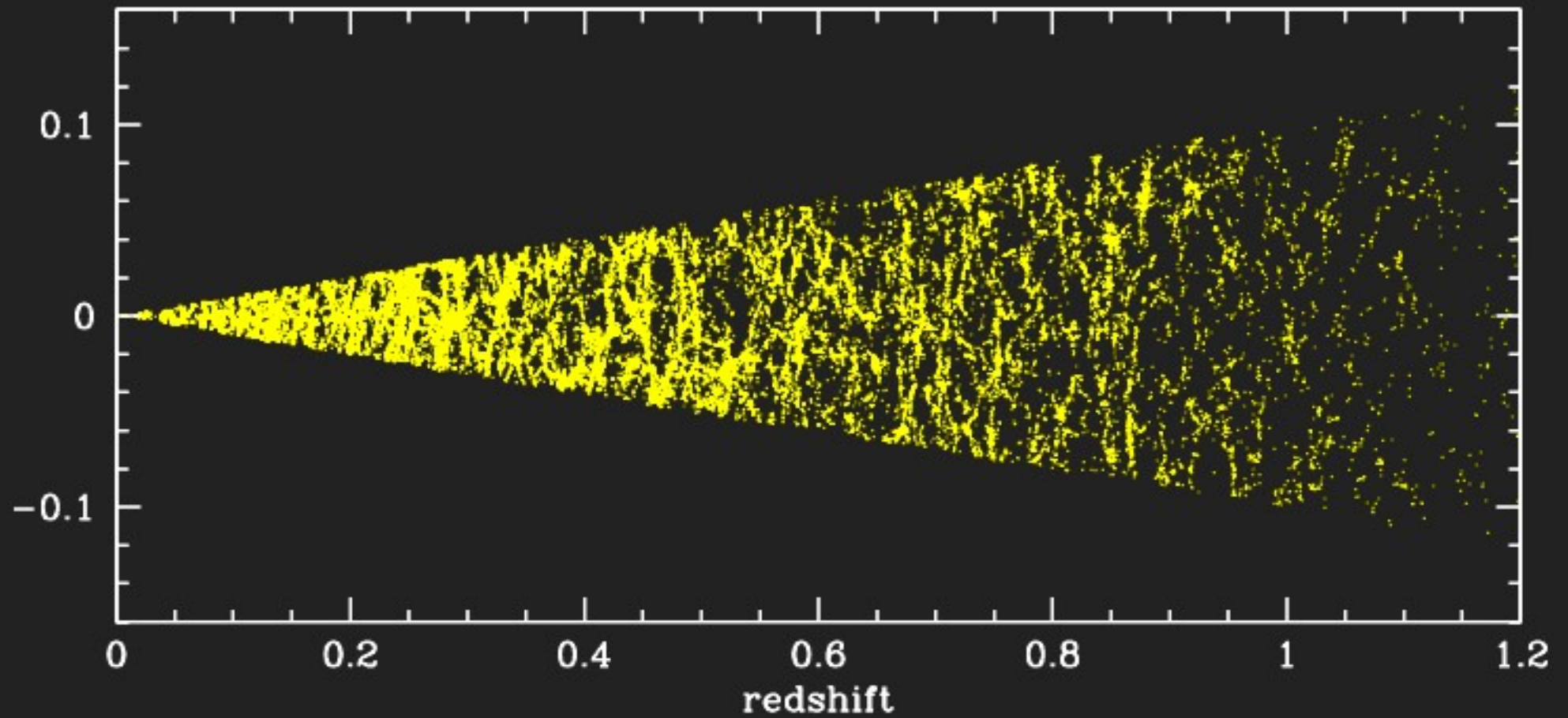


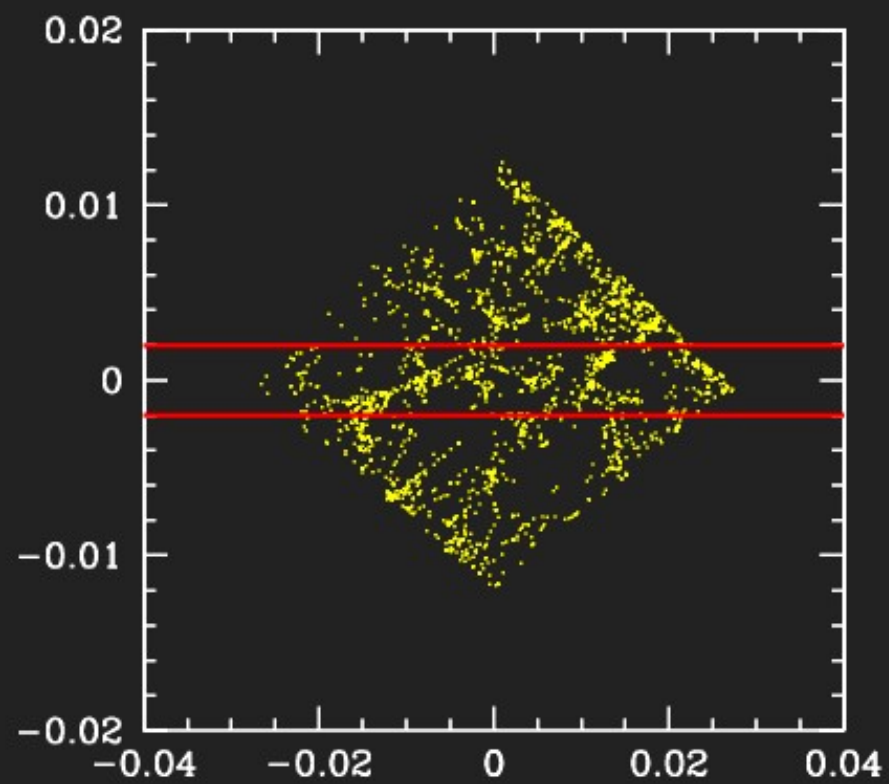
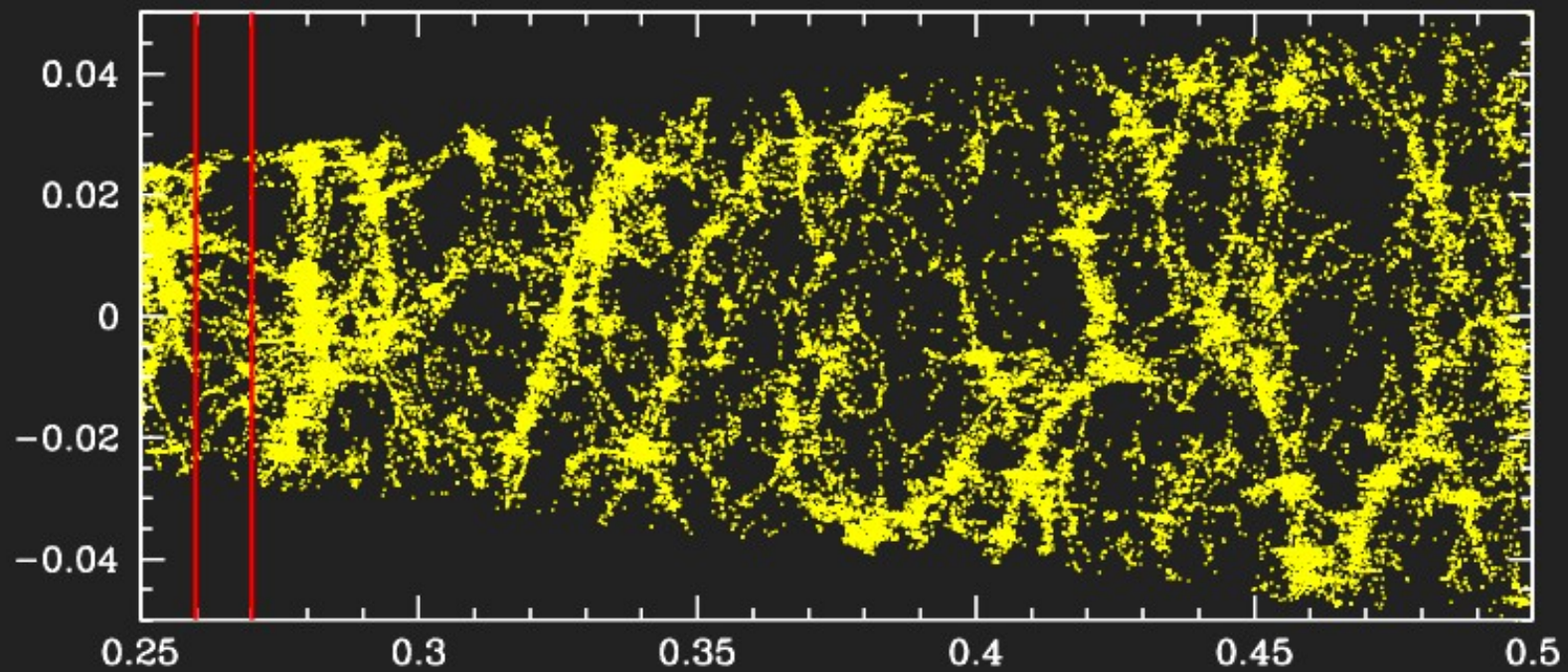
**Kitzbichler & White (2007)**

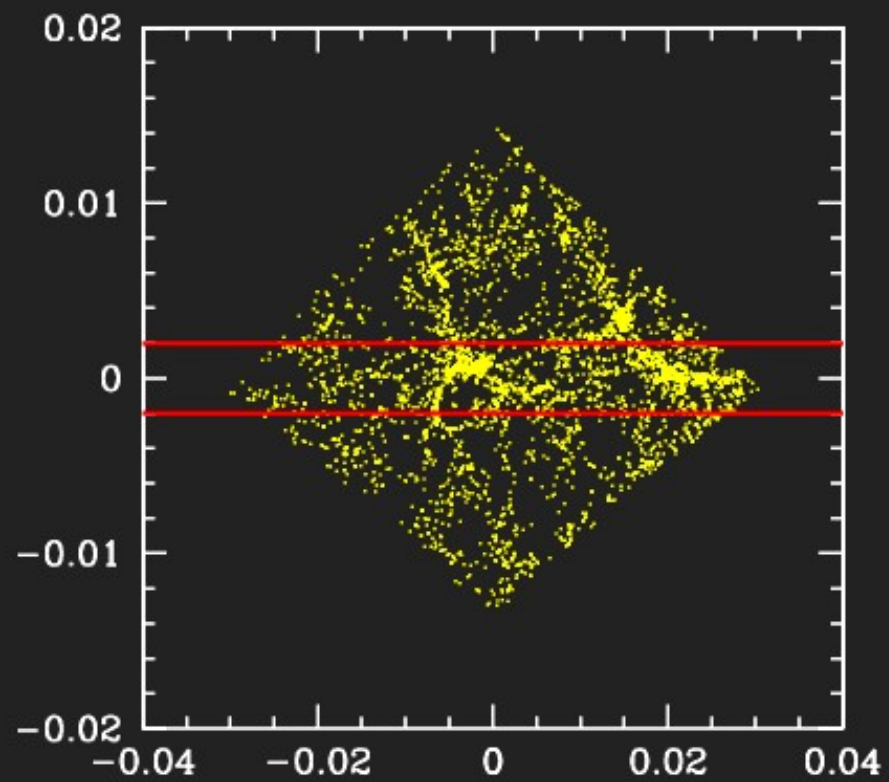
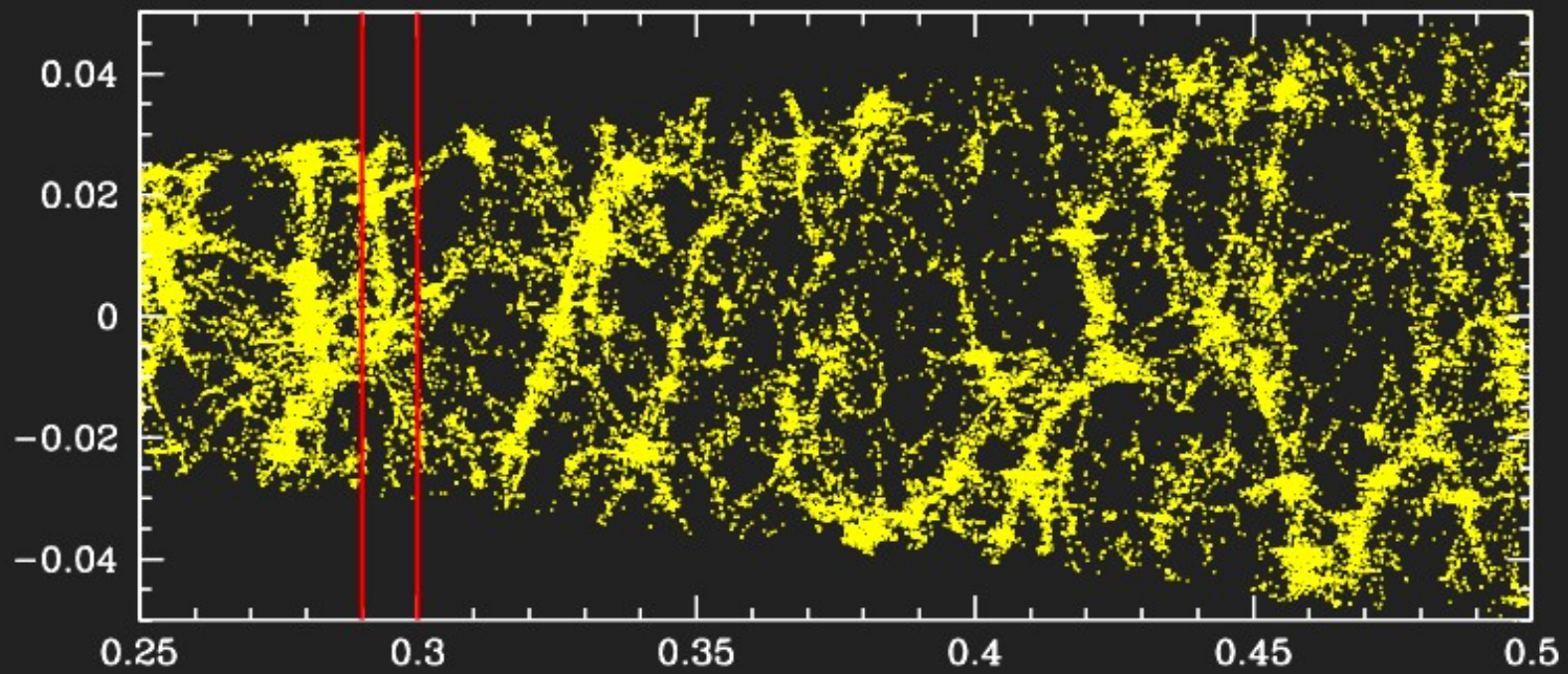
# JPAS observational constraints

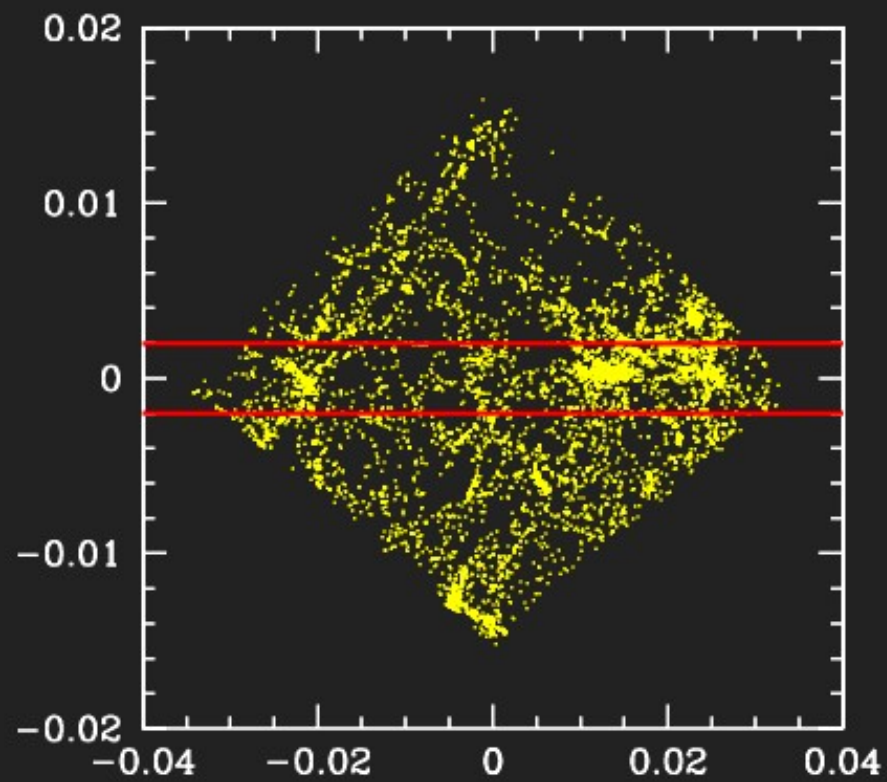
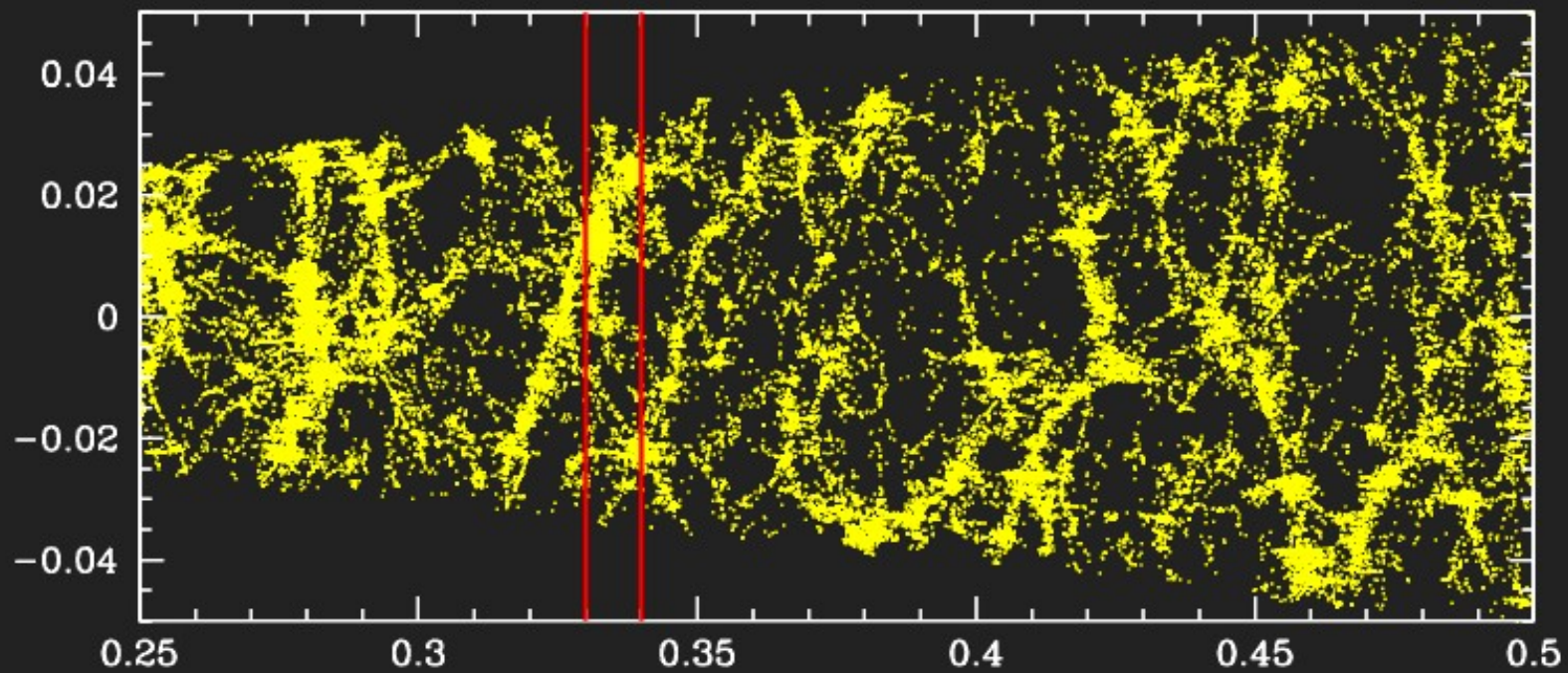
- JPAS will have an *i* broad band magnitude which will be quite similar to the *i*-band of the SDSS.
- The Guo et al. (2011) semianalytical model provides the five SDSS rest frame absolute magnitudes. We use *i*-sdss band to our lightcone.
- We transform to observed apparent magnitudes using a mean *K* correction for the *i* band extracted from Poggianti et al. (1997).
- We include an apparent *i* band limit of 23, similar to the limit in the future JPAS.

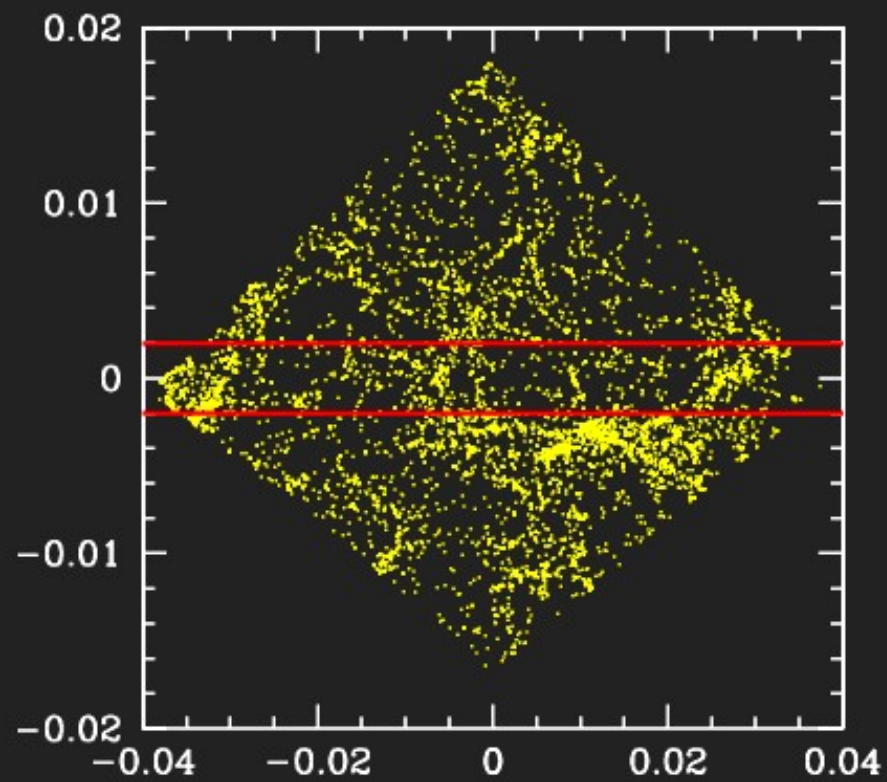
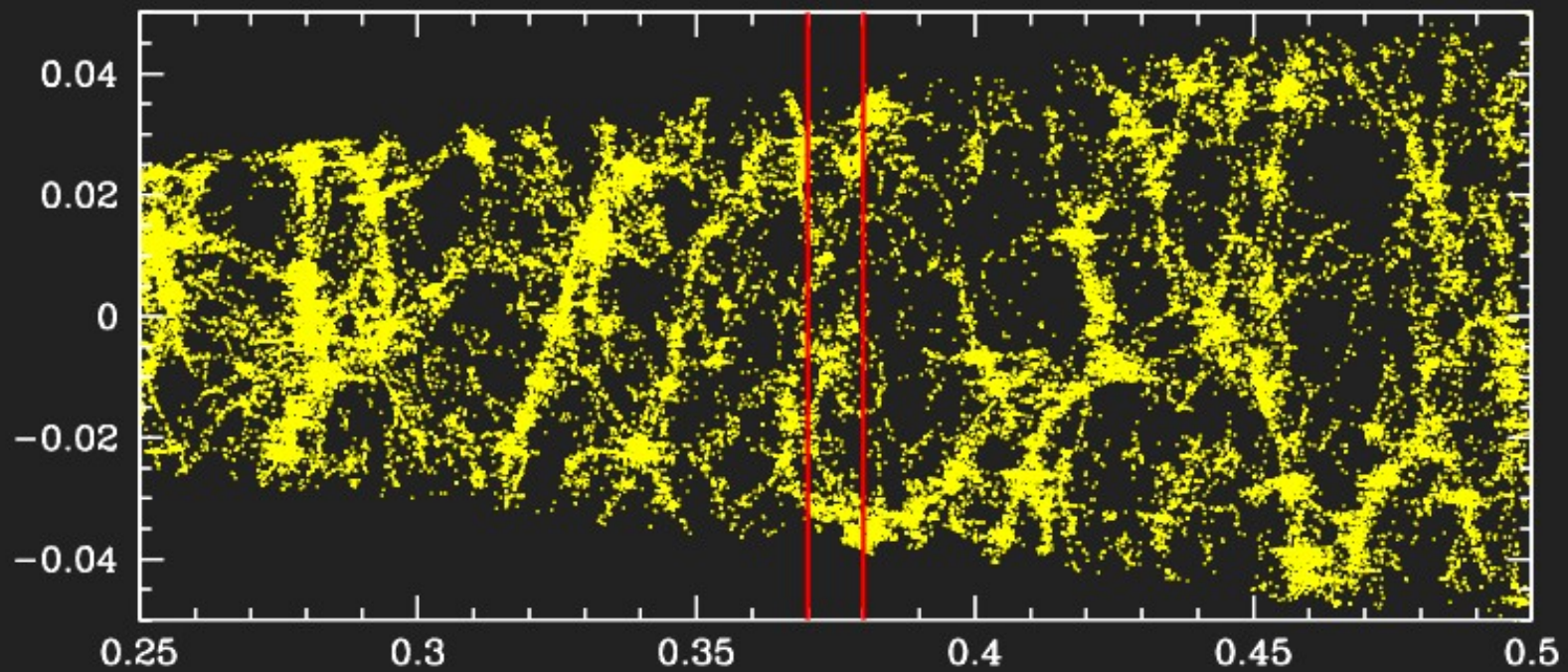
# The Final Lightcone

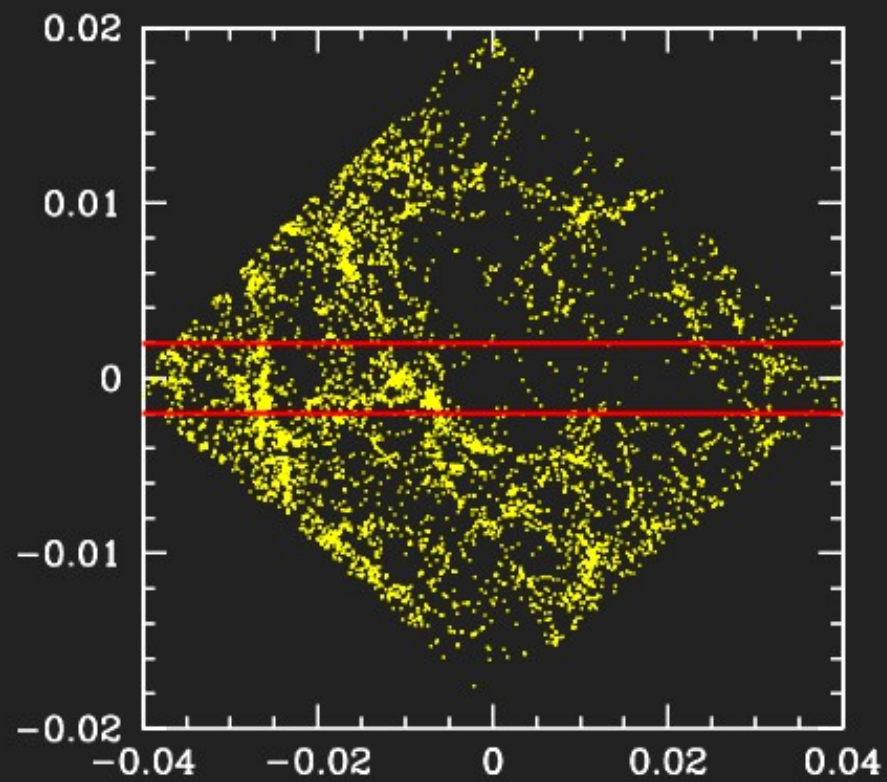
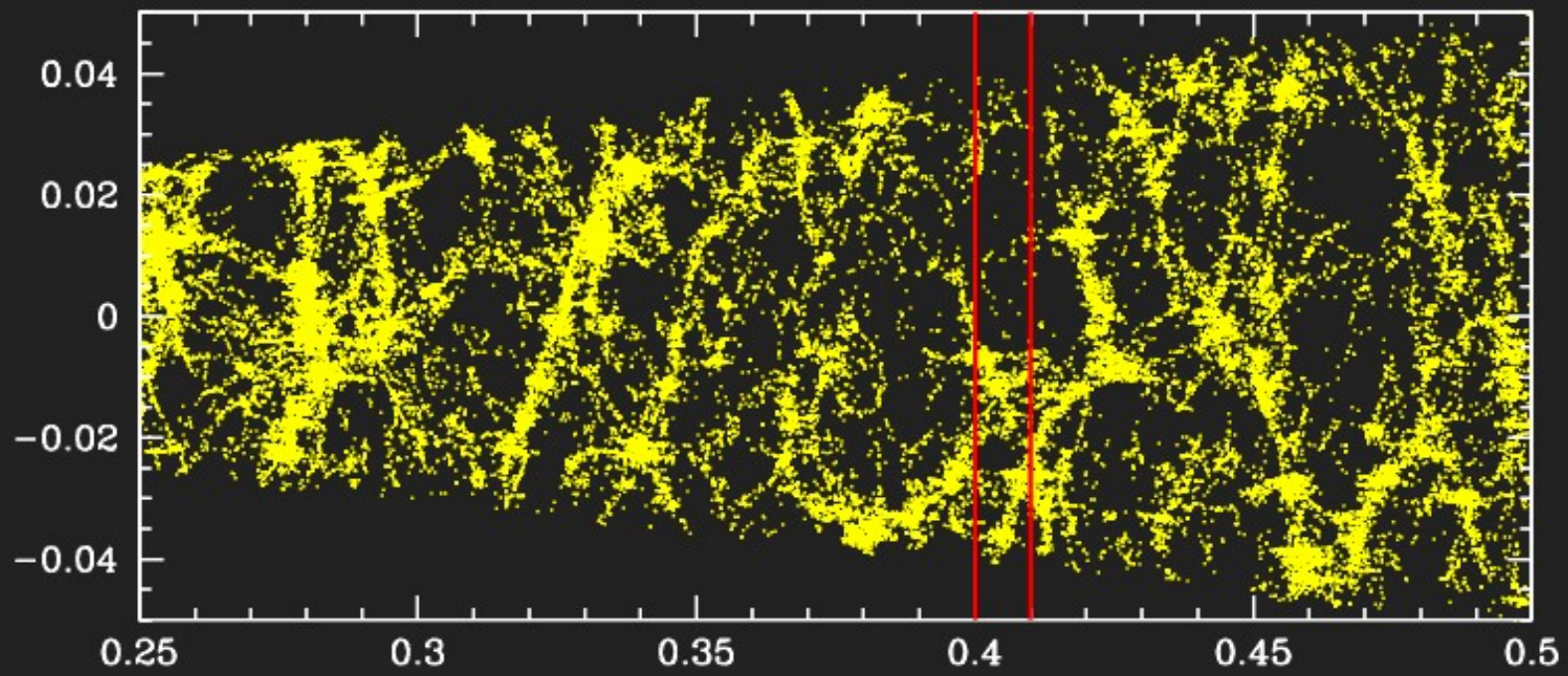




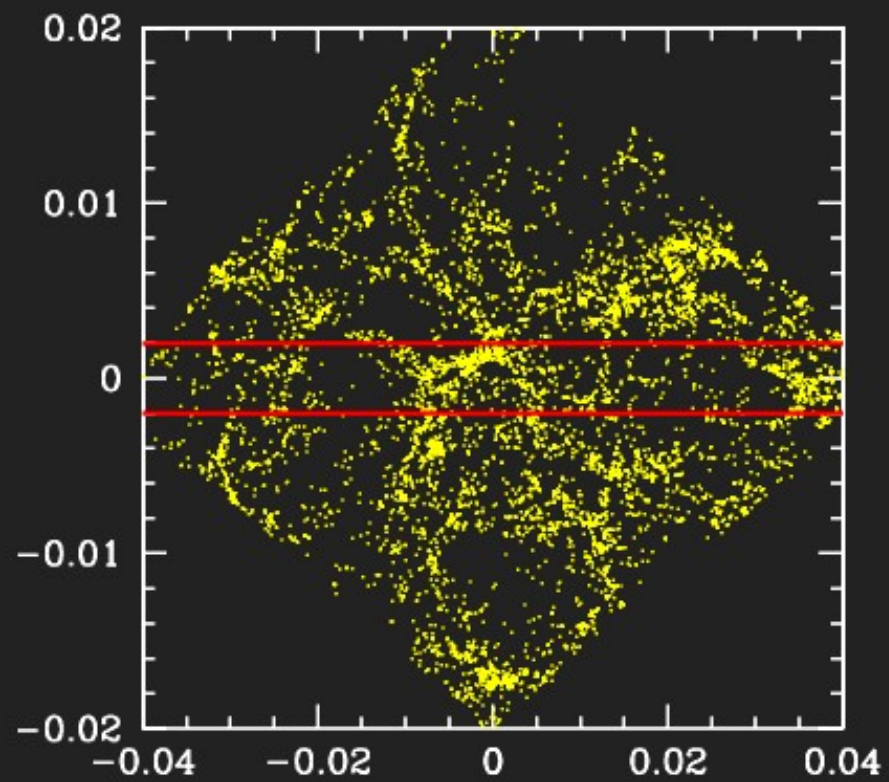
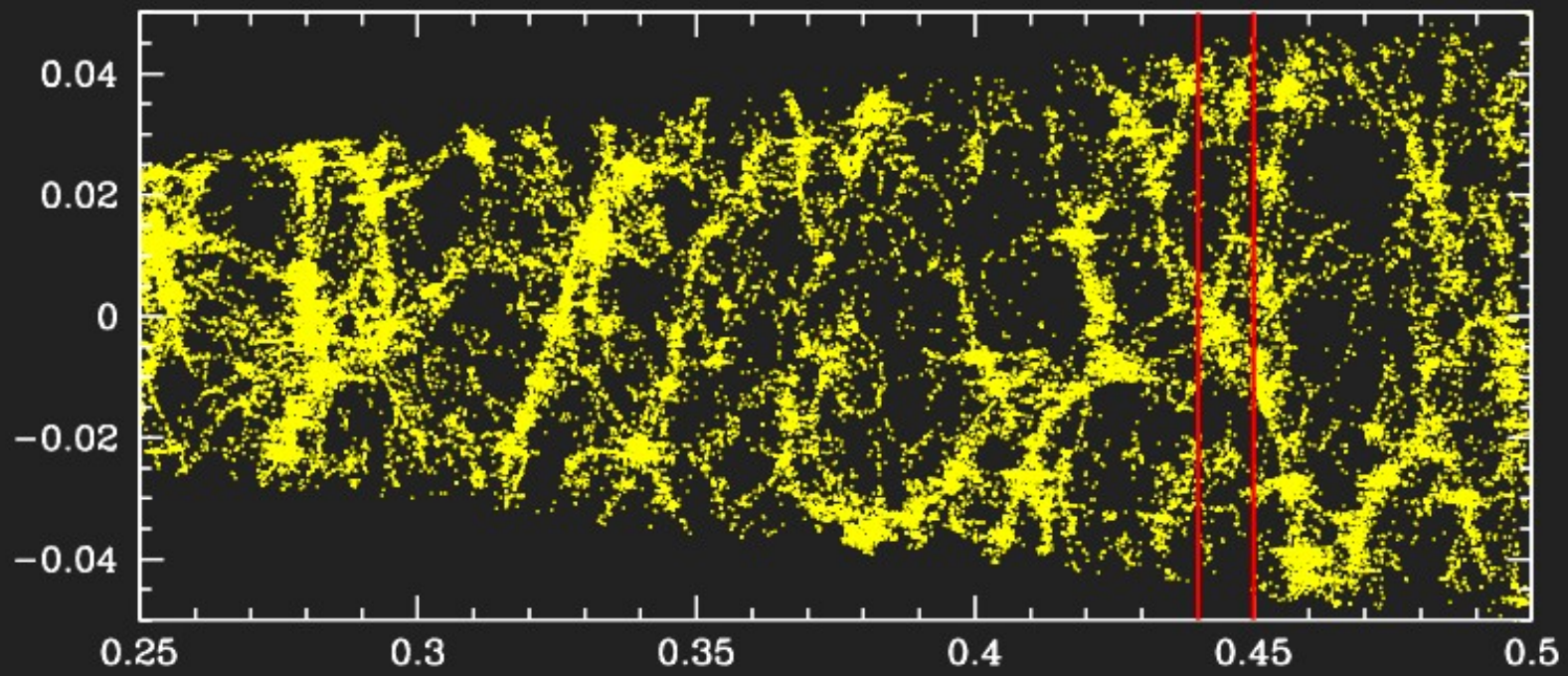


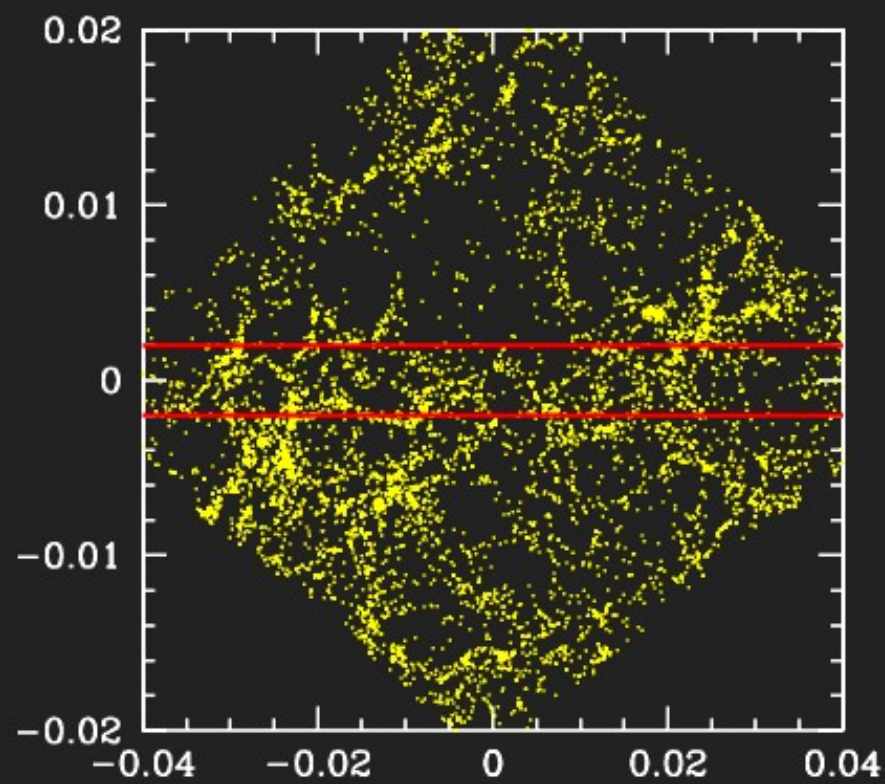
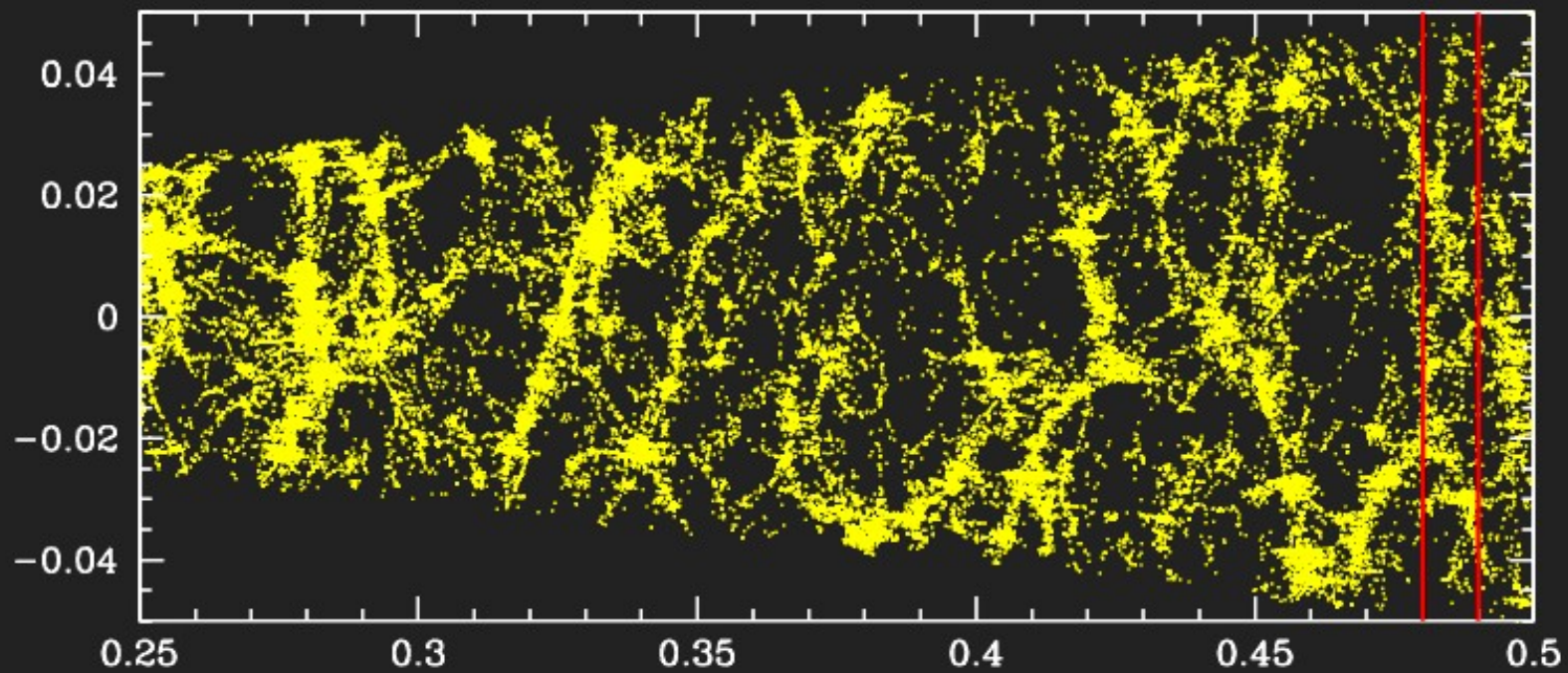












# JPAS lightcone: Results

- **Comprises ~500,000 galaxies**
- **Maximum redshift: 1.2**
- **Angular coverage: ~30 deg<sup>2</sup>**
- **Absolute magnitude limit: -16.4 (i<sub>SDSS</sub> band)**
- **Stellar mass limit: ~ 10<sup>8</sup> h<sup>-1</sup> M<sub>o</sub>**

# Friends of Friends algorithm

**Huchra & Geller (1982)** : Original FoF for observational spectroscopic catalogues.

**Davis et al. (1985), Knebe et al. (2011)** : Modified FoF for 3D simulations.

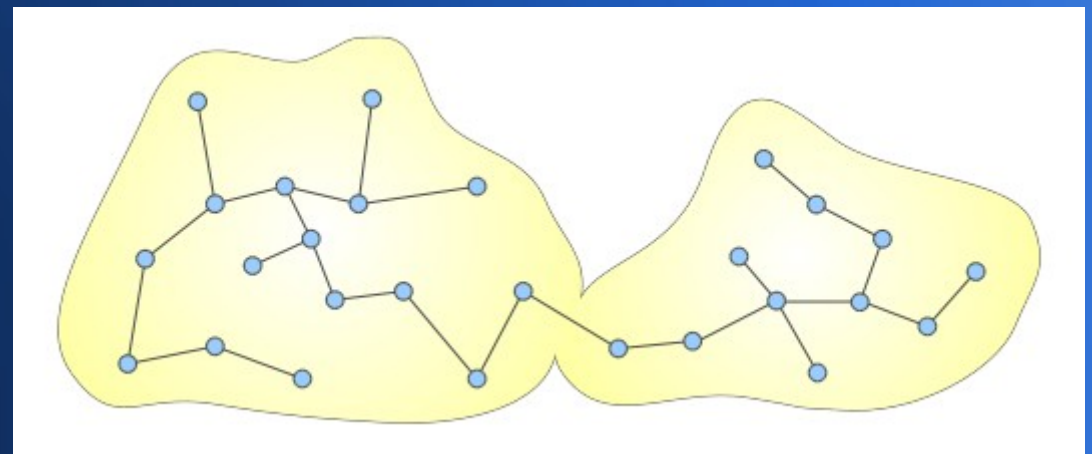
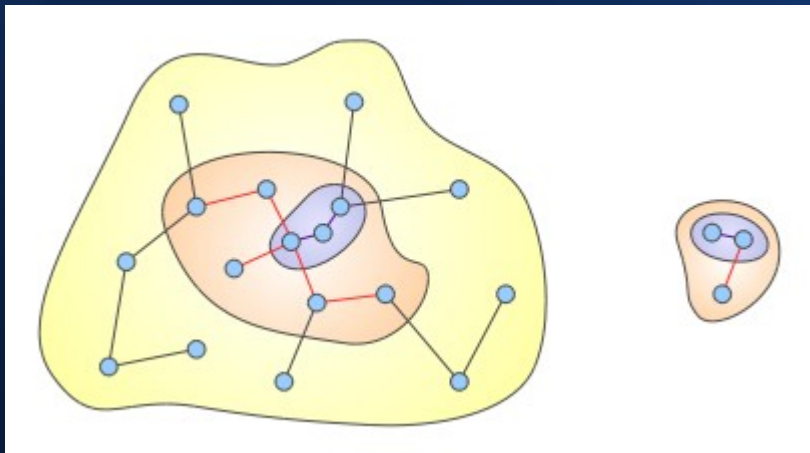
**Merchán & Zandivarez (2002,2005)**: Modified FoF for 2dFGRS & SDSS.

**Botzler et al. (2004), Li & Yee (2008), Liu et al. (2008)**: Modified FoF for photometric catalogues.

**BASIC IDEA** : linking galaxies that share common neighbours (friends). It starts looking for the friends of an initial galaxy that have separations lower than a given threshold. The surroundings of each friend are examined until no more friends are found.

$$D_{ij} \leq D_1 \text{ and } V_{ij} \leq V_1$$

$D_1$  and  $V_1$  are called transversal and radial linking lengths, respectively.



# Ideal group sample

NO flux limit

NO redshift  
distortion

**GROUP REFERENCE SAMPLE** : groups having 4 or more members are identified on the volume limited sample in real space. The linking lengths are specified only by the cosmological model that determines the overdensity of virialization, and the space density of galaxies, both as a function of redshift.

$$D_1 = D_0(z) \text{ and } V_1 = D_1 H(z)$$

Flux limit

NO redshift  
distortion

## **GROUP RESTRICTED-REFERENCE**

**SAMPLE**: is the reference sample only with those galaxies with apparent magnitude  $< 23$ . This is the *ideal* sample that should be identified in a flux limited catalogue.

**In observational samples, there are two main constraints that the algorithm has to take into account:**

- **FLUX LIMIT**
- **REDSHIFT SPACE DISTORTIONS**

**The linking lengths have to be modified!**

**WHICH ARE THE PROPER LINKING LENGTHS,  $D_1$  and  $V_1$ , TO RECOVER THE IDEAL GROUPS WHEN IDENTIFYING IN OBSERVATIONAL CATALOGUES ?**

# Tuning the FoF linking lengths



**FLUX LIMITED SAMPLE** : The linking lengths have to consider the diminishing of the galaxy number density due to the missing faint galaxies. Therefore, the linking lengths depend on the galaxy luminosity function.

$$D_1 = D_0(z) R_s \text{ and } V_1 = D_1 H(z)$$

We tested the algorithm against a fixed luminosity function for nearby galaxies  $LF(0)$ , or a variable  $LF(z)$ . Then,  $R_s(0)$  or  $R_s(z)$ , respectively



NO Flux limit

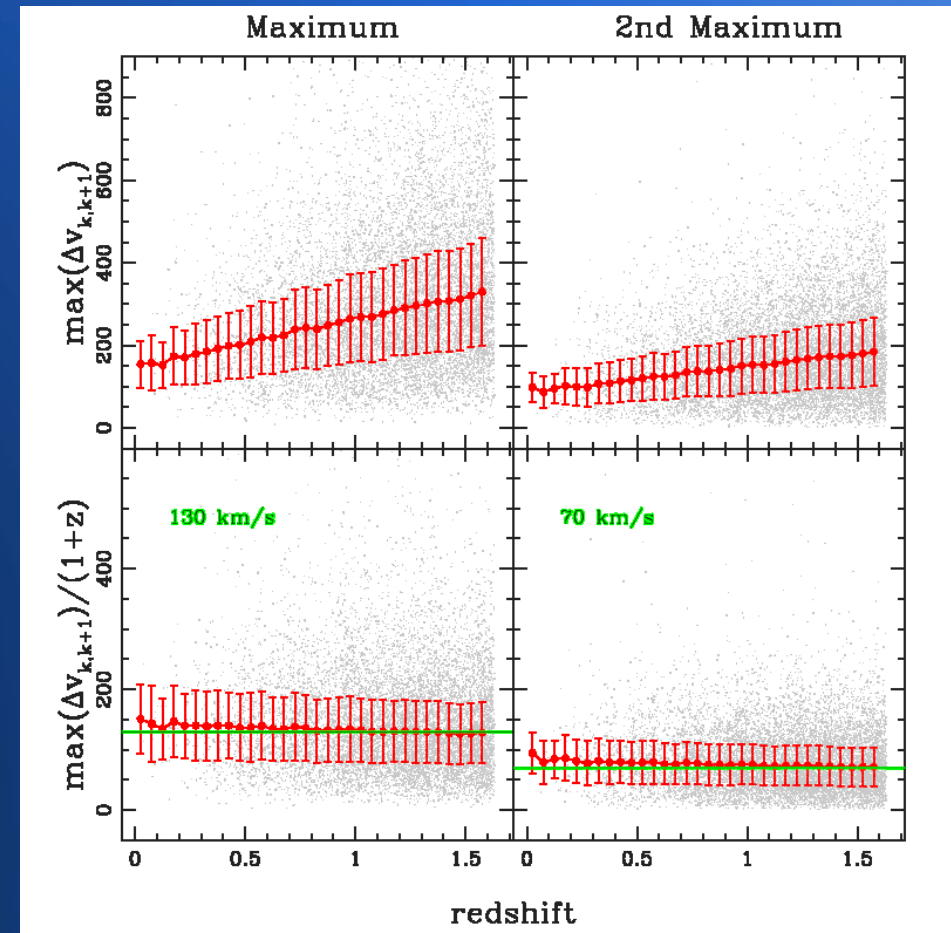
Redshift  
distortion

**REDSHIFT SAMPLE** : The radial linking length has to consider the redshift distortion due to peculiar velocities.

$$D_1 = D_0(z) \quad \text{and} \quad V_1 = V_0$$

We examined the radial distortions of groups in the REFERENCE sample, to look for the most suitable value of  $V_0$  to link all the galaxies in the group.

We analyzed the maximum radial velocity difference between a galaxy and its closest neighbour, and the second maximum per group.



NO Flux limit

Redshift  
distortion

**REDSHIFT SAMPLE** : The radial linking length has to consider the redshift distortion due to peculiar velocities.

$$D_1 = D_0(z) \text{ and } V_1 = V_0$$

We tested the algorithm against four different recipes for  $V_0$  [km/s]

$$V_0 = 130$$

$$V_0 = 130(1+z)$$

$$V_0 = 70$$

$$V_0 = 70(1+z)$$

# Resulting Group Samples

Sample	Linking lengths		Total number of glxs in groups	Groups with $4 \leq N < 10$	Groups with $N \geq 10$
<i>reference</i>	$D_l = D_0(z)$	$V_l = D_l H(z)$	1,825,303	159,258	41,774
<i>restricted-reference</i>			99,230	8,986	2,308
<i>flux limited-LF variable</i>	$D_l = D_0(z) R_s(z)$	$V_l = D_l H(z)$	107,768	10,255	2,446
<i>flux limited-LF fixed</i>	$D_l = D_0(z) R_s(0)$	$V_l = D_l H(z)$	116,777	10,923	2,675
Redshift	$D_l = D_0(z)$	$V_l = 130$	1,287,097	160,145	23,572
	$D_l = D_0(z)$	$V_l = 130(1 + z)$	2,133,189	203,975	46,557
	$D_l = D_0(z)$	$V_l = 70$	629,841	98,537	8,383
	$D_l = D_0(z)$	$V_l = 70(1 + z)$	1,394,091	170,918	26,372
sp-mock catalogue	$D_l = D_0(z) R_s(z)$	$V_l = 130(1 + z) R_s(z)$	120,518	12,694	2,574

# Purity & Completeness

**PURITY :** how good are the identified groups compared to a reference sample?

**COMPLETENESS :** how many of the original reference groups are recovered in the new identification?

## Different categories:

**P1:** 100% Pure

**P2:** >70% Pure, <30%

interlopers

**P3:** mostly mergers + few

interlopers

**P4:** <70% Pure, >30%

interlopers

**P5:** <70% mergers + >30%

interlopers

**P6:** 100% False

**C1:** 100% recovered

**C2:** >70% recovered, <30%

missing glxs

**C3:** split + few missing glxs

**C4:** <70% recovered, >30%

missing glxs

**C5:** <70% split + >30%

missing glxs

**C6:** 100% missing glxs

# Purity & Completeness

Class	Flux limited		Redshift				Sp-mock
	LF variable	LF fixed	$V_0 = 130$	$V_0 = 130(1+z)$	$V_0 = 70$	$V_0 = 70(1+z)$	$V_0 = 130(1+z)$
P1	62	51	42	35	49	42	28
P2	21	24	21	21	20	21	23
P3	1	2	6	5	8	6	3
P4	3	5	12	12	11	12	13
P5	0	0	2	1	1	1	1
P6	13	18	17	26	11	18	32
P1+P2	83	75	63	56	69	63	51
C1	82	89	14	48	3	17	42
C2	12	8	16	25	5	18	27
C3	2	2	6	8	2	7	8
C4	1	0	21	8	19	21	10
C5	0	0	6	1	7	5	1
C6	3	1	37	10	64	32	12
C1+C2	94	97	30	73	8	35	69

# Purity & Completeness

Class	Flux limited		Redshift				Sp-mock
	LF variable	LF fixed	$V_0 = 130$	$V_0 = 130(1+z)$	$V_0 = 70$	$V_0 = 70(1+z)$	$V_0 = 130(1+z)$
P1	62	51	42	35	49	42	28
P2	21	24	21	21	20	21	23
P3	1	2	6	5	8	6	3
P4	3	5	12	12	11	12	13
P5	0	0	2	1	1	1	1
P6	13	18	17	26	11	18	32
P1+P2	83	75	63	56	69	63	51
C1	82	89	14	48	3	17	42
C2	12	8	16	25	5	18	27
C3	2	2	6	8	2	7	8
C4	1	0	21	8	19	21	10
C5	0	0	6	1	7	5	1
C6	3	1	37	10	64	32	12
C1+C2	94	97	30	73	8	35	69



# Purity & Completeness

Class	Flux limited		Redshift				Sp-mock
	LF variable	LF fixed	$V_0 = 130$	$V_0 = 130(1+z)$	$V_0 = 70$	$V_0 = 70(1+z)$	$V_0 = 130(1+z)$
P1	62	51	42	35	49	42	28
P2	21	24	21	21	20	21	23
P3	1	2	6	5	8	6	3
P4	3	5	12	12	11	12	13
P5	0	0	2	1	1	1	1
P6	13	18	17	26	11	18	32
P1+P2	83	75	63	56	69	63	51
C1	82	89	14	48	3	17	42
C2	12	8	16	25	5	18	27
C3	2	2	6	8	2	7	8
C4	1	0	21	8	19	21	10
C5	0	0	6	1	7	5	1
C6	3	1	37	10	64	32	12
C1+C2	94	97	30	73	8	35	69



# Group Spectroscopic Sample

Flux limit

Redshift distortion

**MOCK SP-SAMPLE** : based on a compromise between purity and completeness, the final linking lengths are

$$D_l = D_0(z) R_s(z) \quad \text{and} \quad V_l = 130(1+z) R_s(z)$$

Sample	Linking lengths		Total number of glxs in groups	Groups with $4 \leq N < 10$	Groups with $N \geq 10$		Sp-mock $V_0 = 130(1+z)$
<i>reference</i>	$D_l = D_0(z)$	$V_l = D_l H(z)$	1,825,303	159,258	41,774		
<i>restricted-reference</i>			99,230	8,986	2,308		
<i>flux limited-LF variable</i>	$D_l = D_0(z) R_s(z)$	$V_l = D_l H(z)$	107,768	10,255	2,446		
<i>flux limited-LF fixed</i>	$D_l = D_0(z) R_s(0)$	$V_l = D_l H(z)$	116,777	10,923	2,675		
Redshift	$D_l = D_0(z)$	$V_l = 130$	1,287,097	160,145	23,572		
	$D_l = D_0(z)$	$V_l = 130(1+z)$	2,133,189	203,975	46,557		
	$D_l = D_0(z)$	$V_l = 70$	629,841	98,537	8,383		
	$D_l = D_0(z)$	$V_l = 70(1+z)$	1,394,091	170,918	26,372		
sp-mock catalogue	$D_l = D_0(z) R_s(z)$	$V_l = 130(1+z) R_s(z)$	120,518	12,694	2,574	$70(1+z)$	
						42	28
	P2	21 24	21	21	20	21	23
	P3	1 2	6	5	8	6	3
	P4	3 5	12	12	11	12	13
	P5	0 0	2	1	1	1	1
	P6	13 18	17	26	11	18	32
	P1+P2	83 75	63	56	69	63	51
	C1	82 89	14	48	3	17	42
	C2	12 8	16	25	5	18	27
	C3	2 2	6	8	2	7	8
	C4	1 0	21	8	19	21	10
	C5	0 0	6	1	7	5	1
	C6	3 1	37	10	64	32	12
	C1+C2	94 97	30	73	8	35	69



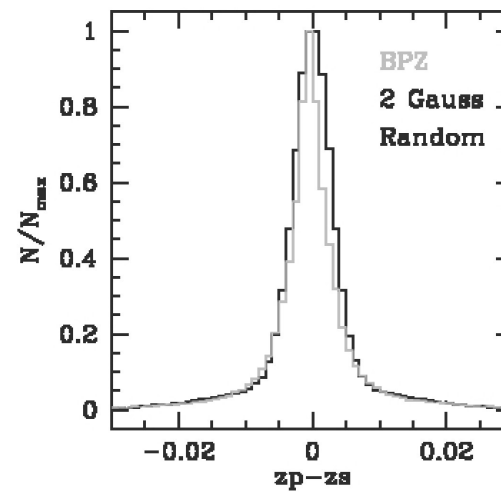
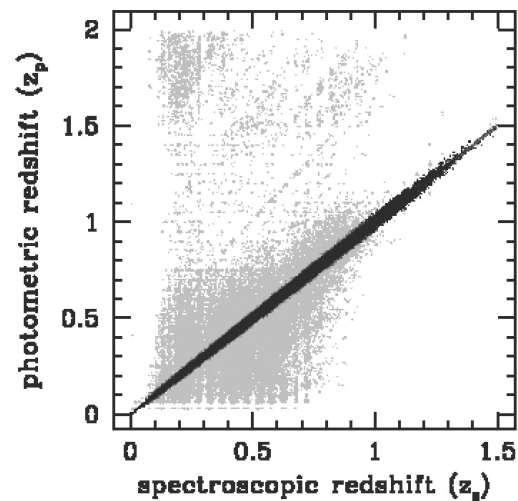
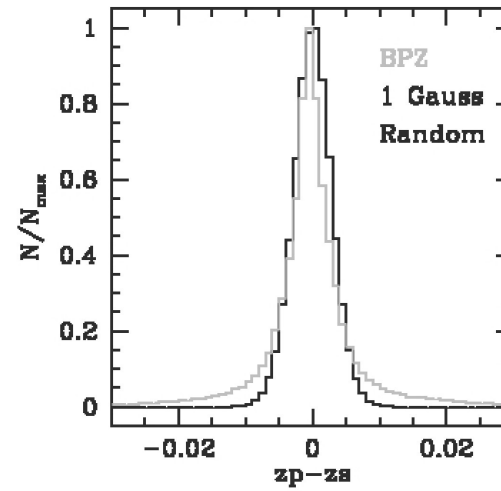
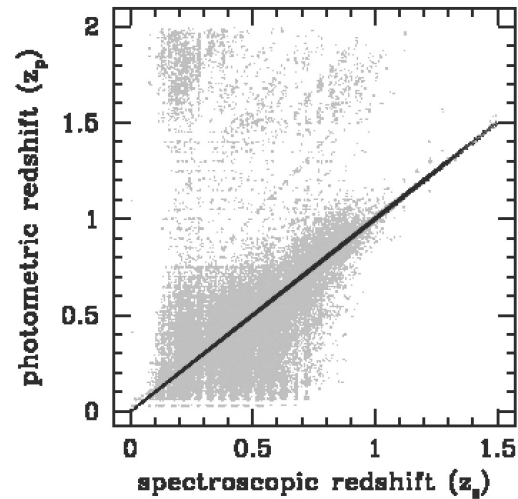
# Identification of groups using photometric redshifts

$$P(|V_2 - V_1| \leq V_l) \equiv \int_0^\infty dz G_1(z) \int_{z-V_l}^{z+V_l} dz' G_2(z')$$

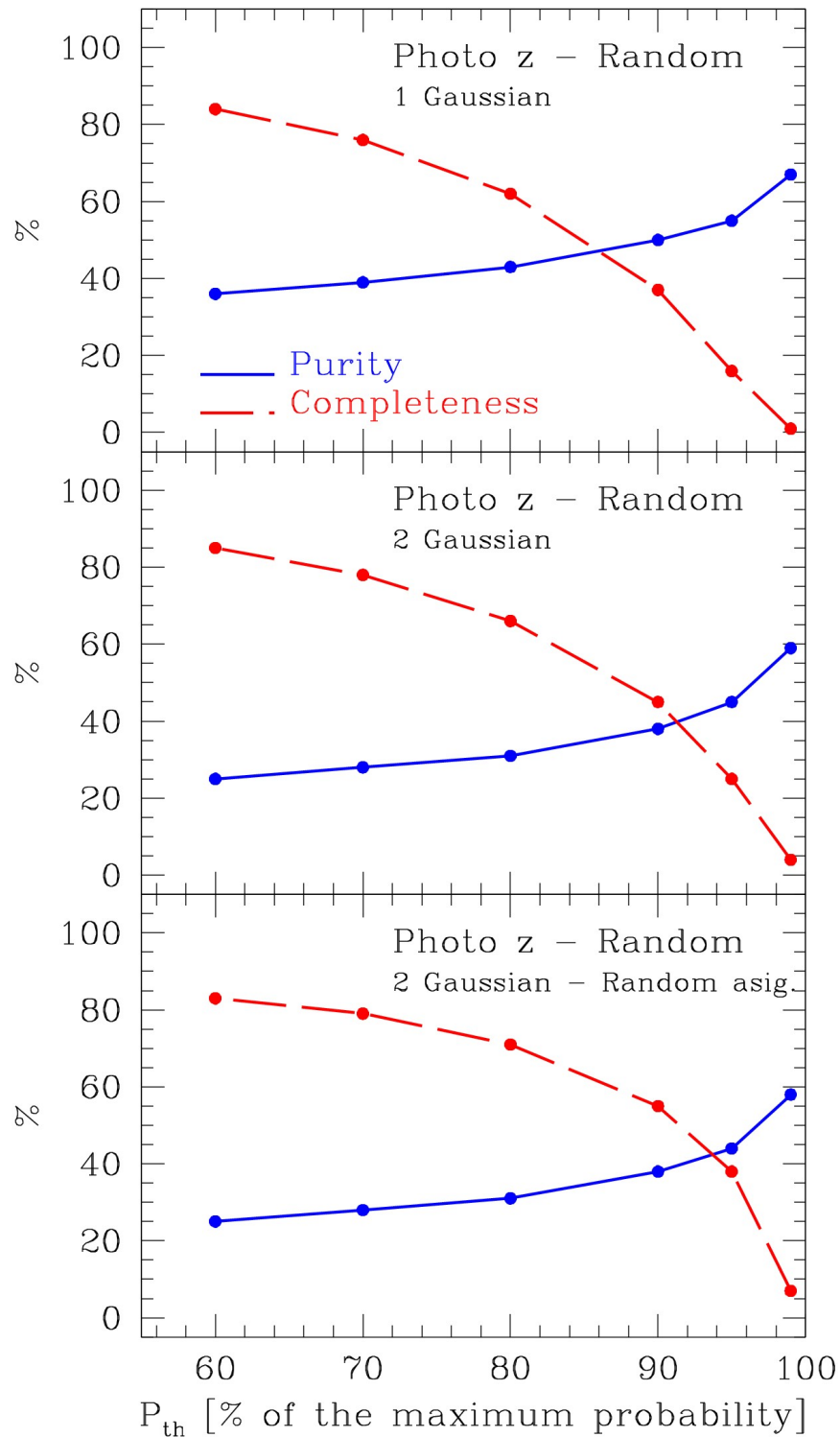
$$P(|V_2 - V_1| \leq V_l) > P_{th}$$

$$G_i(z) = \frac{1}{\sigma_i \sqrt{2\pi}} \exp\left(\frac{-(z - z_i)^2}{2\sigma_i^2}\right)$$

# Identification of groups using photometric redshifts



# Purity and Completeness using random photo-z



# Purity and Completeness using BPZ photo-z

